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An Early Warning System for banking crises: From regression-based analysis to machine learning techniques

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Abstract

Ten years after the outbreak of the 2007-2008 crisis, renewed attention is being directed to money and credit fluctuations, financial crises and policy responses. By using an integrated dataset that includes 100 countries (advanced and emerging) spanning from 1970 to 2017, we propose an Early Warning System (EWS) to predict the build-up of systemic banking crises. The paper aims at (i) identifying the macroeconomic drivers of banking crises, (ii) going beyond the use of traditional discrete choice models by applying supervised machine learning (ML) and (iii) assessing the degree of countries' exposure to systemic risks by means of predicted probabilities. Our results show that the ML algorithm has a better predictive performance than the logit model. Both models deliver increasing predicted probabilities in the last years of the sample for the advanced countries, warning against the possible build-up of pre-crisis macroeconomic imbalances.

Keywords: banking crises; EWS; machine learning; decision trees; AdaBoost.

JEL classification: C40; G01; C25; E44; G21.

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1. Introduction

The 2007-2008 financial crisis that hit advanced economies triggered a worldwide economic downturn with severe and widespread losses across the real and financial sectors. It unfolded as a systemic banking crisis and reinforced the attention of national and supranational institutions on the links between money and credit fluctuations and the insurgence of a crisis, with an eye towards mitigating the propagation of similar crises.

A better understanding of countries' financial vulnerabilities is crucial to contain the contagion effects in case a new crisis should occur. In particular, recognising the economic factors that carry valuable information to identify vulnerabilities is key to developing countries' resilience to economic shocks. The ultimate goal is to design macroprudential policies addressing such vulnerabilities and limit them from building up further and spreading across the economic system.

Against this background, economists have developed Early Warning Systems (henceforth, EWSs) aimed at detecting the risks that a systemic banking crisis may arise. This literature has evolved following various approaches, from the signals approach to discrete choice models and machine learning techniques. Kaminsky and Reinhart (1999) and Kaminsky (1999) represent one of the first contributions using the signals approach. Further work along this line is provided by Borio and Lowe (2002) and Davis and Karim (2008), among others. Demirgüc-Kunt and Detragiache (1998) make use of logit models and were followed by contributions analysing different subsets of countries and periods (e.g. Arteta and Eichengreen, 2000, Demirgüc-Kunt and Detragiache, 2005, Barrell et al., 2010, and Schularick and Taylor, 2012). More recently, machine learning methods have been employed by economists to improve the predictive performance of EWSs. Duttagupta and Cashin (2011) and Alessi and Detken (2018) implement these modelling techniques to analyse banking crises. Another example in this direction is Manasse and Roubini (2009) on sovereign debt crises.

This empirical literature stems from – and partially overlaps with – a wide field of research aimed at identifying banking crisis episodes, according to a variety of criteria. Demirgüc-Kunt and Detragiache (1998) build on the first attempts in the literature (e.g. Lindgren et al., 1996; Caprio and Klingebiel, 1997) and identify banking crisis episodes based on the occurrence of a number of disruptive events related to the banking sector. More recently, Laeven and Valencia (2018), evolving from their previous work, put forth a more sophisticated definition of systemic banking crises.

With this paper, we contribute to the literature by developing an EWS for advanced and emerging economies. Our goal is threefold. First, to identify macroeconomic indicators that could contain valuable information to uncover vulnerabilities leading to a banking crisis should an economic shock occurs. Second, to propose an EWS by using both a modelling technique taken from machine learning, namely Adaptive Boosting (AdaBoost), and from traditional econometrics, namely the logit model. Third, to combine the output from both methodologies to provide the necessary tools to predict the build-up of a banking crisis.

For these purposes, we collect information on banking crisis episodes from various sources to maximise coverage across both time and countries. The banking crisis dataset is then merged with information on selected macroeconomic indicators. In particular, we select variables that have been suggested to serve as leading indicators of banking crises by similar research. We end up with an integrated dataset that includes 100 countries – 33 advanced and 67 emerging – over the period 1970-2017.

Our work brings a number of novelties to existing research. First, we combine banking crises and macroeconomic information from different sources and we update them according to the latest

available data. Second, we put together different lines of research and attempt to shed light on the most meaningful leading indicators of banking crises. Third, we adopt the AdaBoost modelling technique to develop an EWS, which to the best of our knowledge, has never been done so far. By doing so, we overcome some of the limitations of traditional regression analysis, especially its predictive performance, while still retaining some of its advantages, namely ease of use and interpretation.

Our results are promising. Overall, the AdaBoost shows a higher predictive performance than the logit model. Both models deliver increasing predicted probabilities in the last years of the sample, warning against the possible build-up of pre-crisis macroeconomic imbalances.

The remainder of the article is organised as follows. Section 2 reviews the literature on the definition of systemic banking crises and on the empirical analyses that aim at predicting them by means of EWSs. Section 3 provides a discussion on how to build an appropriate binary variable employable as target variable in the empirical applications. In Section 4, we show some stylized facts on banking crises and macroeconomic contexts. In Section 5 we estimate an EWS by means of logit models. Section 6 introduces the main features of supervised machine learning methods. In Section 7 we implement an EWS by applying a supervised ML algorithm, i.e. Adaptive Boosting and we show its predictive performance and compare it with that of the logit model. Section 8 concludes with a summary of the main findings.

2. Review of the literature

The widespread losses of the 2007-2008 global financial crisis in the advanced economies brought to the forefront the need for an effective Early Warning System (EWS) to help governments and international financial institutions act promptly to prevent risks of possible future bank runs and bank failures from turning into a systemic banking crisis.

The literature on how to identify, explain and predict "crises" has a long-lasting tradition. In the last two decades – and with renewed attention in the last one – the focus has shifted from balance of payments and currency crises to systemic banking crises. The definition of banking crises is not straightforward and economists provide different criteria to identify their occurrence (Section 2.1). The literature also provides ways to link macroeconomic imbalances with crisis episodes, to explore their role as leading indicators and to assess the ability of econometric models to predict banking crises or the risks that a crisis may occur (Section 2.2).

2.1 The definition of systemic banking crises

There is a wealth of definitions of banking crises. Baron et al. (2018) suggest a classification of the approaches to identify them: (i) the "policy-based" approach (Caprio and Klingebiel, 1997 and 2003; Demirgüc-Kunt and Detragiache, 1998 and 2005; Laeven and Valencia, 2008, 2013 and 2018) and (ii) the "narrative-based" approach (Bordo et al., 2001; Reinhart and Rogoff, 2009 and 2011; Schularick and Taylor, 2012; Jordà et al., 2017a).

Demirgüc-Kunt and Detragiache (1998) observe that the most dated literature (among others, see Lindgren et al., 1996; Caprio and Klingebiel, 1997) provides an overview of banking sector fragility, but does not always distinguish either financial distress from banking crises or local crises from systemic crises. They take from these studies to build a new framework to classify an episode of distress as a

¹ For details on how Caprio and Klingebiel (1997) define banking crises, see **Table A1**.

systemic banking crisis. This is based on four conditions: excessive level of nonperforming assets (NPAs) to total assets, substantial rescue operations, large-scale nationalization of banks, and finally bank runs and deposit freezes (see **Table A1** for details). If at least one of these events occurs, they define the episode of distress as a systemic banking crisis. They apply their definition to 29 countries for the years 1980-1994, identifying 31 crisis episodes.

More recently, Laeven and Valencia (2008) and subsequent updates (Laeven and Valencia, 2013 and 2018) put forth a more articulated definition of systemic banking crises, adding on what proposed by Demirgüc-Kunt and Detragiache (1998). They identify a banking crisis when losses are severe, i.e. a high level of nonperforming loans (NPLs) to total loans or relevant fiscal restructuring costs. However, if these losses are mitigated by policy intervention or it is difficult to quantify them, they look at whether three out of six measures were implemented (four of them are partially retrieved from Demirgüc-Kunt and Detragiache, 1998) (see **Table A1** for details). If this happens, the episode of distress is defined as a systemic banking crisis. Their most recent database covers 165 countries over the period 1970-2017 and identifies 151 crisis episodes.²

The policy-based approach requires richness of data and economic-related information to identify banking crises, causing limited time and country coverage. This prompted a new strand of the literature, the narrative-based approach, which refers to narrative sources of events such as bank runs or policy intervention, to identify banking crisis and fill-in the gaps and extend coverage of the policy-based approach. This approach gives the opportunity to include a number of banking crises backed by a strong historical narrative that are "forgotten" in the policy-based framework (Baron et al., 2018).

Reinhart and Rogoff (2011) provide the first systematic contribution in this direction. They extend preliminary analysis of economic historians such as Bordo et al. (2001) for the pre-World War II period, while take from Caprio and Klingebiel, (1997 and 2003) for the post-1970 period. In their study, a banking crisis is identified when bank runs lead to the closure, merging, or takeover by the public sector of one or more financial institutions. If there are no bank runs, crises are marked by events such as the closure, merging, or takeover by the public sector of an important financial institution that later spread to other financial institutions (see **Table A1** for details). Their database spans from 1800 to 2009, covers 70 advanced and emerging countries and identifies 290 banking crises.³

In line with these studies, Schularick and Taylor (2012, p. 1038) define financial crises as "events during which a country's banking sector experiences bank runs, sharp increases in default rates accompanied by large losses of capital that result in public intervention, bankruptcy, or forced merger of financial institutions". In their view, banking crises are credit booms gone bust. Their final dataset is the result of a critical scrutiny and merge of previously compiled datasets (i.e. Bordo et al., 2001; Laeven and Valencia, 2008; Reinhart and Rogoff, 2011) and covers 70 countries for the period 1870-2008 (**Table A1**). Jordà et al. (2017a) update this dataset, extending the analysis to 17 countries up to 2013 (**Table A1**).

According to Baron et al. (2018), both approaches suffer from some shortcomings. The narrative-based one may be biased because it takes account only of the most relevant events, while the policy-based one because the policy intervention response may be endogenous, subjective and not always timely. To overcome what they think is a subjectivity bias they adopt an alternative approach by using a "hard" measure such as countries' bank equity index and by developing a crisis indicator based on

² Their dataset is complemented with 236 currency crises and 74 sovereign debt crises.

³ They also identify 209 sovereign default episodes.

the decline in the index to refine the chronology of banking crises (see **Table A1** for details). Their database consists of 113 crisis episodes, for 46 countries over the period 1870-2016.

The resulting variable of all the approaches is a binary variable (0/1), where the 1s define systemic banking crisis episodes and the 0s all the other periods. This variable is used as the outcome or target variable in most of the models of the EWS literature.

2.2 The prediction of banking crises by EWSs

Besides monitoring the occurrence of banking crises, building a variable that identifies these episodes is functional to the "estimation" of empirical models – EWSs – aimed at detecting the risks that a systemic banking crisis may arise. The literature on EWSs has evolved along different lines, from the signals approach to discrete choice models and to machine learning techniques.

The signals approach is a non-parametric method, which studies the ex-post behaviour of macroeconomic variables and verifies whether the indicators follow a pattern in the pre-crisis periods that differs from that in tranquil or normal times. A variable is considered to signal a crisis if it exceeds a pre-defined threshold.⁴ Kaminsky and Reinhart (1999) are the first to apply this approach to balance of payments and banking crises for a number of industrial and developing countries for the period 1970-1995, covering 76 currency crises and 26 banking ones.

However, with the signals approach each indicator is used in isolation and the model does not allow the aggregation of the individual warnings. The simplest solution consists of counting the number of leading indicators signalling distress. Nonetheless, this statistic "may not be the best choice because the economy may be vulnerable, but still many of the indicators may not signal jointly that something is wrong" (Kaminsky, 1999, p. 23). Kaminsky (1999) develops, among others, a composite index that weights the signals of each variable by the inverse of their noise-to-signal-ratio to account for the forecasting accuracy of each variable. Borio and Lowe (2002) and Davis and Karim (2008) take from here and apply this methodology to banking crises, for the time spells 1960-1999 and 1979-2003, respectively.

An alternative methodology that allows the simultaneous study of macroeconomic variables as determinants of banking crises is the logit model, a tool widely used in microeconometrics to estimate the probability of an event. The outcome variable is binary (crisis/non-crisis) and the probability that the event (crisis) occurs is estimated as a function of macroeconomic factors. From the estimated coefficients of the model, it is possible to retrieve the estimated probabilities of the crisis. Demirgüc-Kunt and Detragiache (1998) apply this method to a large sample of developed and developing countries in 1980-1994 and find that the main determinants of a banking crisis are low growth, high inflation and high real interest rates. The literature evolved along these lines, with contributions from, among others, Arteta and Eichengreen (2000), Demirgüc-Kunt and Detragiache (2005), Barrell et al. (2010) and Schularick and Taylor (2012) for a variety of countries and time spells.

Although these papers employ the same econometric approach and discriminate between the crisis episodes (1) and all other periods (0), they may differ in what they classify as 0s. The non-crisis years

⁴ Thresholds are discretional and based on the distribution of the variable of interest.

⁵ In a binary classification problem, the noise-to-signal ratio is defined as the ratio between (i) the ratio of the number of crises incorrectly predicted to all non-crisis episodes (false positive rate) and (ii) the ratio of the number of crises correctly predicted to all crisis episodes (sensitivity or true positive rate). The lower the noise-to-signal ratio associated with a variable, the better the ability of the variable to predict a crisis.

are a non-homogeneous informative set since they encompass a mix of time spells with different characteristics – pre-crisis, post-crisis and normal (or tranquil) times.

A widely used method consists of dropping some of the non-crisis years. Demirgüc-Kunt and Detragiache (1998) follow two approaches, one in which they drop all the observations following the first crisis episode experienced by a country and one in which they exclude the post-crisis years. Demirgüc-Kunt and Detragiache (2005) apply the latter criterion. Arteta and Eichengreen (2000) drop the three years before and after the crisis and therefore the 0s denote tranquil times only. Conversely, Barrell et al. (2010) and Schularick and Taylor (2012) make no distinction among pre-, post-crisis and normal times and thus they use the 0s as indicators of all the non-crises years. More recently, Fielding and Rewilak (2015) estimate a dynamic probit model in which the post-crisis years are classified as 1s. The explanatory variables set includes not only the lags of the macroeconomic factors, but also the lagged outcome variable, with the aim of quantifying the persistence of the crisis.

Hardy and Pazarbasioglu (1999) and Caggiano et al. (2014) explicitly address the issue that post-crisis years may differ significantly from times of normality, i.e. they tackle what Bussiere and Fratzsche (2006) – in studying currency crises – label "post-crisis bias". Therefore, their target variable is not binary, but takes on three values. In both papers, the value 0 identifies tranquil times. They differ in how they classify the other two values. In the former, 1 identifies the pre-crisis years and 2 the crisis years, while in the latter, 1 labels the crisis year and 2 the crisis years other than the first. Given the nature of the dependent variable, in both cases, the methodology adopted is a multinomial logit.

In most of these studies, the explanatory variables are taken in lags, since the objectives of the analysis are (i) to build an EWS to link pre-crisis macroeconomic imbalances to the crisis episodes, and (ii) to perform forecasts to predict the risks that a crisis may arise in the future, should these imbalances occur again.

The use of discrete outcome models is widely accepted and employed in the literature. Despite they are not structural macroeconomic models – but reduced-form models – they allow an economic interpretation of the links between the outcome variable and the explanatory variables through their estimated signs and coefficients. Like any standard econometric technique, logit models heavily depend on data availability, particularly in cases where the analysis covers a wide range of countries. They are also best kept relatively simple for ease of interpretation. Most importantly, they are not optimised to solve prediction problems (Kleinberg et al., 2015), which instead is the focus of EWS. To overcome these shortcomings, economists are increasingly employing machine learning (ML) methods in empirical works where the main objective is to perform predictions (for a review, see Athey, 2018). ML (or rather "supervised" ML) is a data mining tool able to (i) analyse complex datasets, (ii) fit multifaceted and flexible functional forms to the data and (iii) find functions that perform well out-of-sample (Mullainathan and Spiess, 2017).

As regards the prediction of crises, Manasse and Roubini (2009) employ a Classification and Regression Tree (CART) to study sovereign debt crises in 47 emerging economies for the period 1970-2002. In Duttagupta and Cashin (2011) banking crises are analysed by means of a Binary Classification Tree (BCT). The paper covers 50 developing and emerging countries, with data from 1990 to 2005. Alessi and Detken (2018) implement the Random Forest (RF) algorithm and apply it to banking crises in the European Union (EU), UK, Denmark and Sweden by using quarterly data from 1970 to 2013.

3. The banking crisis dataset and the target variable

To identify a banking crisis, we start from Laeven and Valencia (2008) and subsequent updates (Laeven and Valencia, 2013 and 2018). This allows us to detect 97 crisis episodes for 100 countries, over the period 1970-2017. To identify additional crisis episodes, we merge information from further sources that apply different criteria to detect a banking crisis. We retrieve (i) 43 additional crisis episodes from Reinhart and Rogoff (2009) and (ii) 1 additional crisis episode from Jordà et al. (2017a). Our final dataset contains 141 crisis episodes, covering 100 countries between 1970 and 2017 (33 advanced economies and 67 emerging ones, see **Table A2** for the complete list). This dataset is the basis of our empirical analyses of Section 5 and Section 7.

3.1 Target variable: crisis vs pre-crisis

After having defined what a banking crisis is and identified the crisis episodes, we turn our attention to the construction of the target variable employed in our empirical analyses. The literature adopts two different approaches: one that aims at predicting the exact occurrence of a crisis (see, among others, Demirgüc-Kunt and Detragiache, 1998 and 2005; Schularick and Taylor, 2012; Richter et al., 2017), and one that aims at signalling the building up of macroeconomic imbalances that may lead to a crisis (e.g. Alessi and Detken, 2018). In the former, the target variable is the crisis itself, while in the latter the target variable consists of the pre-crisis periods.

Since our interest lies in building an early warning system that may help anticipate the occurrence of a crisis, we follow the second approach both in the econometric analysis (Section 5) and in machine learning (Section 7).⁶ For this reason, we need a definition of the pre-crisis years. Following Arteta and Eichengreen (2000), we label the three years preceding each banking crisis "pre-crisis". Moreover, we label the three years following each banking crisis "post-crisis". Finally, the time spells that are at least three years past a crisis and at least three years prior to a subsequent crisis are classified "normal times". Therefore, in addition to the crisis episodes, our sample is partitioned into three intervals: pre-crisis, post-crisis and normal (or tranquil) times (**Table 1**).

TABLE 1 ABOUT HERE

Table 2 and **Table 3** display the occurrence of crises, pre- and post-crisis episodes and normal times, for a selection of advanced and emerging economies, respectively. When due to the frequent occurrence of a crisis, a post-crisis period overlaps with the pre-crisis period of a subsequent crisis, we give priority to the post-crisis episode. Therefore, it may happen that we do not observe a pre-crisis spell before a crisis (for instance, for the the USA between 1984 and 1988), or that a period of normality is shorter than the predefined three-year spell (i.e. Japan between 1992 and 1997).

TABLE 2 and 3 ABOUT HERE

Over the whole period, we observe 55 banking crises for the 33 advanced economies and 87 for the 67 emerging economies. Among the advanced economies, all countries recorded at least a crisis episode, with the exception of Hong Kong. The UK is the one with the highest number of crises (five), followed by the USA, Iceland and Korea with three. Nineteen crises (35% of the total) occurred

⁶ In the econometric analysis, we also show the results of logit models in which the target variable is the crisis.

⁷ For the sake of brevity and readability of the tables, we selected twenty advanced economies and twenty emerging ones based on their contribution to world GDP, with the exception of Kazakhstan, Russia, Ukraine and Hungary, which are listed because they are the only emerging countries in which we record a crisis in 2007 or after.

between 2007 and 2008. Among the emerging economies, sixteen countries did not experience any crisis consistent with the definition adopted in this paper. The distribution of the crises is much more disperse than among developed countries and shows the highest concentration of episodes in the 1990s. Only four economies (Kazakhstan, Russia, Ukraine and Hungary) experienced a banking crisis in 2008.

Targeting either the crisis or the pre-crisis years entails three definitions of the outcome variable. In all three cases, it continues to be a binary (0/1) variable (**Table 4**). In Approach 1, the value 1 identifies the crisis, while the value 0 all other periods. In Approach 2, the target variable equal to 1 identifies the pre-crisis spells. However, we have two options in defining the 0s. We either include (definition 2a) or exclude (definition 2b) the post-crisis episodes.

In line with Demirgük-Kunt and Detragiache (2005) and to avoid the post-crisis bias, we adopt definition (2b) and drop the post-crisis periods from the definition of the 0s. We use this characterisation of the target variable in our main specifications of the empirical analyses of Section 5 and Section 7. For comparison purposes, Section 5 also presents a model in which the outcome variable is defined according to Approach 1. The two approaches imply a different set of explanatory variables. In Approach 1, the occurrence of the crisis is explained by previous-period macroeconomic factors, while in Approach 2 all factors are contemporaneous with the pre-crisis period.

TABLE 4 ABOUT HERE

4. Descriptive statistics

The banking crisis dataset of Section 3 is merged with the macroeconomic indicators listed in **Table A3** in the Appendix. We select these variables as previous literature suggests that they could contain valuable information to identify vulnerabilities that may lead to a banking crisis. For this reason, they are used as explanatory variables in the empirical applications of Section 5 and Section 7. As our precrisis indicator is at the yearly level, we gather macroeconomic data on a yearly basis. Worthy of note is that we collect information from different data sources. To have the widest possible coverage across both time and countries for a single indicator, we combine consistent data from different sources when needed. For instance, we complement data on credit-to-GDP from the Bank of International Settlement (BIS) with information taken from the World Bank (WB). We provide the surface of the control of th

The selected variables can be grouped in two sets according to their level of detail: (i) country-specific and (ii) global. As to the former, we identify a few macroeconomic fundamentals, in particular the current account balance as a share of GDP, external debt-to-GNI and public debt as a ratio of GDP. Richter et al. (2017) for example stress how a larger current account deficit indicates increased financial flows from abroad, which might increase financial fragility because of possible capital flow reversals. We also control for external and public debt as a proxy for countries' solvency and liquidity (Manasse and Roubini, 2009). Countries with lower levels of public debt are expected to be less fragile and thus, better able to counteract the emergence of a banking crisis. Moreover, higher levels of external debt may indicate a country's greater integration in the world economy making it more vulnerable to external shocks.

⁸ Barbados, Belize, Suriname, Trinidad and Tobago, Syria, Brunei, Pakistan, Botswana, Gabon, Libya, Mauritius, Seychelles, Namibia, Fiji, Turkmenistan and finally Serbia and Montenegro.

⁹ With the exception of the VIX. See the text for details.

¹⁰ In some cases, we are still left with some missing values. If gaps are sparse, we recover the missing values by interpolation.

As our focus is on banking crises, we choose two banking variables taken from the literature on credit booms. The first one is credit-to-GDP, while the second is bank credit-to-bank deposits. According to this line of research, excessive credit growth is a sign of an overheated economy that, if hit by an adverse shock, could trigger a banking crisis. However, Schularick and Taylor (2012) and Richter et al. (2017), find weak evidence that excessive credit growth poses a threat to financial stability. Furthermore, we employ bank-credit-to-bank deposits as a measure of aggregate liquidity of the banking sector. Jordà et al. (2017b) find that this indicator increases prior to banking crises and enhances the risk of credit booms ending badly.

We consider an additional set of indicators, namely inflation, the real effective exchange rate and an openness index. As suggested by Demirgüc-Kunt and Detragiache (1998), inflation may provide indications of macroeconomic mismanagement, which adversely affects the economy. The real effective exchange rate is added following Gourinchas and Obstfeld (2012) who find that this indicator is particularly relevant to predict financial instability in emerging economies. Local currency depreciations should increase the vulnerability of those countries holding foreign-denominated debt. We also account for the degree of openness of a country. More open economies may be more exposed to financial fragilities coming from abroad.

The last country-specific variable refers to asset prices, more specifically the real house price index. Recent literature stresses that house price booms are a key vulnerability of modern economies, especially in times of "credit bubbles" (Jordà et al., 2015). In this framework, we follow Alessi and Detken (2018) who include property prices, among other variables, to build an early warning system to predict banking crises.

Our second set of indicators provides information on a global scale. These include the 10y US treasury rate, a composite energy price index, real world GDP growth and the VIX. The 10y US Treasury rate is meant to highlight vulnerabilities affecting emerging economies especially. In particular, tight monetary conditions in the US may reduce capital flows to emerging economies and thus contribute to their debt servicing difficulties (Manasse and Roubini, 2009). By deteriorating the balance of payments of highly import dependent countries, the change in energy prices may provide information on the resilience of an economy to adverse exogenous shocks. Finally, the conditions of the global economy as a whole are captured by the real growth of world GDP and the VIX. These variables may have an ambiguous explanatory effect on financial instability. For example, high real GDP growth rates may signal either overheating or a buoyant economic environment. Likewise, the VIX is a measure of market perceived volatility in either direction.

4.1 Data manipulation

Before proceeding, it is important to describe how we prepare the data for the next steps of our analysis. As for the country-specific variables, we treat the data in the following way. The indicators expressed as year-on-year percentage changes are used as they are, namely inflation, the real effective exchange rate and the house price index. Each of the other time series is detrended using a two-sided Hodrick-Prescott (HP) filter and standardised (i.e. we subtract the country specific mean and divide by the standard deviation). Detrending allows us to remove the time trend and capture the cyclical component, while the standardisation smooths heterogeneities between countries and across time. Overall, the detrending and standardisation allow us to compare the behaviour of diverse variables across different countries.

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¹¹ In the HP filter, we use a smoothing parameter equal to 100 as the periodicity of our data is yearly.

Regarding the set of variables at the global level, we only work on the VIX as the other indicators are expressed as rates. ¹² As for the VIX, we need to translate it into a yearly indicator as we gather data points on a daily basis. ¹³ We take both the maximum value observed in each year as well as the annual average of the collected daily data points.

4.2 Crisis, pre-crisis and the macroeconomy

Table 5 presents summary statistics of the control variables for the group of advanced and emerging economies separately. Additionally, it presents the means of the raw and transformed version of the indicators used in the analysis, discriminating between means in the full sample ("Overall"), and the means for the four sub-periods described in Section 3.1. At the bottom of the table we report means for the detrended and standardised variables. In the following we focus on the raw variables as the transformed one have mean equal to 0 by construction and convey the same kind of information when looking at differences between sub-periods. Two main observations follow.

TABLE 5 ABOUT HERE

First, there is a significant difference in a number of country-specific variable means between advanced and emerging economies in the full sample, as shown by the t-test reported in **Table 6**. This further justifies our choice to keep the two groups separate in our analysis. Current account deficits are larger in emerging economies, which puts them in a more vulnerable position compared to advanced economies. External debt-to-GDP and the openness index are relatively high in advanced economies. This result is not surprising as advanced countries are usually more integrated in the global economy compared to the developing world. Heterogeneities are also present with regards to the means associated to the banking variables, especially credit-to-GDP. It suggests that in emerging economies the banking sector is not as developed as in the other group of countries and that banking crisis are less likely to be triggered by an overheated credit market. Moreover, inflation is much higher in emerging economies. Although this result is partly due to countries experiencing significant inflationary pressures, prices are generally much more volatile in emerging countries than in developed ones.¹⁴

TABLE 6 ABOUT HERE

Second, the path of means from tranquil times to the outbreak of the crisis is consistent with expectations. Most of the selected macroeconomic variables indicate a worsening of the macroeconomic situation in the run up to the crisis. For example, current account deficits deteriorate as we approach the crisis. External debt-to-GDP is relatively low in normal times and it increases as we move towards the outbreak of the crisis. For emerging economies inflation increases substantially in the wake of the crisis and more so in the midst of the crisis. Banking variables increase as we approach the crisis but only for developed countries. Overall, this suggests that we correctly classified the four sub-periods. Yet, only a few of the selected macroeconomic variables improve in the post-crisis period. Moreover, a number of indicators present a similar behaviour to that exhibited in the pre-crisis period. Thus, to avoid any confounding factors that could affect our results, we exclude the post-crisis years from the analysis of Sections 5 and 7.

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¹² The energy price index and the real world-GDP growth are expressed as year-on-year percentage changes.

¹³ In particular, we collect the daily closing prices of the VIX.

¹⁴ In our dataset there are 123 observations with inflation higher than 100% and, with the exception of 6 observations (Israel between 1980 and 1985), they belong to the group of emerging economies.

Next, we look at the distribution of normal times, pre-crisis and crisis plus post-crisis years according to the quartile of each of our explanatory variables. This type of analysis allows us to identify which of the macroeconomic variables are more useful to detect vulnerabilities that may precede a crisis. Also, we acknowledge that the set of relevant variables may differ between advanced and emerging economies. For this reason, we continue to keep the two subsamples separate.

Figure 1 draws attention to a selection of macroeconomic indicators that, more than others, carry information on the existence of macroeconomic imbalances in the years prior to a crisis. Worthy of note is that the frequencies associated with pre-crisis years are relatively low, while the tranquil times represent the majority of the observations. **Panel (a)** shows that in developed countries current account deficits are associated with a higher occurrence of pre-crisis periods. As the current account balance improves (we move from the first to the fourth quartile), pre-crisis years are less common. For emerging economies, instead, no clear pattern emerges.

FIGURE 1 ABOUT HERE

A comparison of **panel (c)** and **panel (d)** shows that high levels of inflation is particularly informative for emerging economies. The two upper quartiles are characterized by a higher frequency of pre-crisis periods compared to the two lower quartiles. In developed countries, however, no clear pattern emerges. As regards the credit-to-GDP and bank credit-to-bank deposit ratio, the occurrence of pre-crisis periods increases with the value of these two banking variables. This evidence is especially visible for developed economies (**panel e** and **panel g**).

A number of additional variables provide insights on countries' vulnerabilities.¹⁵ In developed economies the external debt-to-GDP presents a higher number of pre-crisis occurrences in the upper tail of its distribution. Meanwhile, pre-crisis periods in emerging economies are more common in the lower tail. As for the real house price index, the majority of pre-crisis periods are concentrated in the last quartile of its distribution in both developed and emerging economies. Public debt-to-GDP, instead, presents a higher occurrence of pre-crisis years in the first quartile, especially for developed countries. Regarding the real effective exchange rate and the openness index, no relevant evidence emerges.

Summarizing, a number of interesting insights emerge from this descriptive analysis. Current account deficits are usually associated to increased vulnerabilities that may lead to a banking crisis. The same applies to hyperinflation, especially for emerging economies. In developed economies, macroeconomic imbalances are associated with overheated credit and housing markets as well as high levels of external debt-to-GDP ratios. In the next sections, we aim at corroborating these results by employing machine learning and econometric techniques.

5. Logit models: Estimation results and predictive performance

The first step of our analysis consists of applying standard econometric techniques to identify the macroeconomic indicators that significantly affect the likelihood of the occurrence of a banking crisis or a pre-crisis period, according to the specification. In particular, we estimate a pooled logit model as follows:

$$Prob(y_{it} = 1|X_{it}) = \frac{\exp(\alpha_i + X_{it}\beta)}{1 + \exp(\alpha_i + X_{it}\beta)}$$
(1)

¹⁵ For this final set of macroeconomic indicators, we do not report the corresponding graphs for the sake of brevity. However, results are available upon request.

where $Prob(y_{it}=1|X_{it})$ denotes the probability that country i in year t is in a crisis or pre-crisis state, X_i is a set of regressors and α_i are geographic dummies. We run three specifications of Equation (1) in line with the definition of the target variable provided in Section 3.1. According to the outcome variable, the information set included in X_i is taken either at time t-1 or at time t. Moreover, we apply the model to the subsample of developed and emerging economies separately, as we acknowledge heterogeneities between the two groups of countries. In particular, we recognize that in developed and emerging economies vulnerabilities are produced by a different set of macroeconomic factors.

Before presenting the results, some clarifications are in order. First, the selection of regressors to include in Equation (1) is heavily affected by data availability across both time and countries. For instance, the VIX time series starts from 1992 and house prices are available only for a subset of countries. If these indicators are plugged in the model they would greatly reduce the sample size thereby jeopardizing the validity of our results. Another reason why we can only include a limited number of indicators in our set of explanatory variables is that we need to attenuate potential correlation and endogeneity bias. In our framework, correlation and endogeneity stem from the fact that macroeconomic indicators react in unison to large scale events, such as banking crises, or show a similar behaviour in the run up to a crisis. We therefore opt to include only the most meaningful country specific macroeconomic indicators disclosed by the descriptive analysis above plus a number of controls at the global level.

Second, in the logit model, as in any non-linear model, estimated coefficients are not directly interpretable. Therefore, we show the derived marginal effects, which allow us to quantify changes in probabilities when a regressor changes by one unit.¹⁸

5.1 The logit models results

Table 7 and **Table 8** present the results for the subsample of advanced and emerging economies, respectively. The models for the sample of developed countries include country dummies, while those for the group of developing countries include region dummies. ¹⁹ Standard errors are clustered at the country level to account for any leftover serial correlation among observations belonging to the same cluster.

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¹⁶ See **Table A2** in the Appendix for the complete list of countries included in our dataset. The sample of advanced economies includes 33 countries observed over the period 1970-2017 for a total of 1,584 observations. We drop Estonia, Hong Kong, Israel, Lithuania and Singapore (240 observations in total) as a complete time series for the selected macroeconomic indicators is not available. We end up with 51 crisis episodes and 1,293 non-crisis episodes. The sample of emerging economies includes 67 countries observed over the period 1970-2017 for a total of 3,216 observations. We observe 87 crisis episodes and 3,129 non-crisis episodes.

¹⁷ The set of explanatory variables for developed economies includes: current account-to-GDP, external debt-to-GNI, public debt-to-GDP, credit-to-GDP. For emerging economies, we replace credit-to-GDP with inflation following the findings emerging from the descriptive analysis of Section 4.

¹⁸ In our framework, a positive (negative) coefficient means that higher levels of the associated macroeconomic indicator increases (decreases) the probability of observing a crisis or pre-crisis period, according to the specification.

¹⁹ We are forced to include region dummies, instead of country dummies, for the subsample of emerging economies, as a significant number of these countries did not experience a banking crisis. In particular, Barbados, Belize, Botswana, Brunei, Fiji, Gabon, Iran, Libya, Mauritius, Namibia, Pakistan, Serbia, Seychelles, Suriname, Syria, Trinidad and Tobago and Turkmenistan. We clustered emerging economies in the following regions: Africa, Asia, the Balkans & East Europe, Caribbean, Central America, Central Asia, East Asia, Latin America, Middle East, North Africa, Pacific and South Asia.

In both tables, in Column (1) the outcome variable identifies the year when the crisis occurs, in line with Approach 1 of **Table 4**. The explanatory variables are taken at time t-1, as it is reasonable to assume that banking crises at time t are generated by previous year macroeconomic imbalances. The dependent variable in Column (2) identifies the pre-crisis periods and corresponds to the outcome variable of Approach 2(a). From Column (3) to (5) the outcome variable identifies the pre-crisis periods but post-crisis periods are excluded from the 0s, in line with Approach 2(b). This is our preferred outcome variable as it drops observations that may suffer from the post-crisis bias (Bussiere and Fratzsher, 2006). For these last set of regressions, the explanatory variables are taken at time t. For each specification, we also report the Area Under the Receiver Operating Characteristic curve (AUROC), a standard measure used to evaluate the predictive performance of a logit or, more generally, any classification model. 21

Overall, the logistic regression confirms the evidence emerging from the descriptive statistics. In advanced economies, the occurrence of a crisis is significantly associated to higher levels of external debt (**Column 1** of **Table 7**). Meanwhile, the likelihood of experiencing a crisis falls as public debt increases. A possible interpretation of this result is that a pre-crisis period could be characterized by a decrease in public debt-to-GDP thanks to GDP growth and pro-cyclical improvement of the primary balance, while when the crisis brakes out, fiscal measures implemented by government could burden public debt. We also find that higher levels of current account deficits and credit-to-GDP increase the probability of observing a crisis, although only the latter is statistically meaningful. As for the global variables, the probability of the occurrence of a crisis increases with the 10y US Treasury rate and world GDP growth. This result provides evidence that, similarly to what we expect for emerging economies, US monetary policy produces imbalances leading to a crisis in advanced economies as well, while world GDP growth could increase crisis probability by fostering a worldwide easing of credit standards and a growing inter-dependence among countries. The same kind of information is conveyed when we look at the probability of being exposed to pre-crisis periods (**Column 2**).

TABLE 7 ABOUT HERE

These findings are robust to the exclusion of the post-crisis periods (**Column 3**). Noteworthy is the improvement in the predictive performance of the model, measured by the AUROC at the bottom of the table, as we move from the second to the third specification that is, when we drop observations corresponding to the post-crisis periods. This result suggests the presence of post-crisis bias in our data.

We enhance the model of Column 3 by adding the interaction between external debt and the 10y US Treasury rate (**Column 4**). Previous results are confirmed, with the exception of the coefficient associated with external debt, which loses statistical significance. Another control we perform is to plug in Equation (1) the maximum value of the VIX observed at time t (**Column 5**). The negative sign associated with the VIX suggests that we cannot consider this variable as a leading indicator. In this case, increased volatility does not translate in increased vulnerability. Worth mentioning is the high predictive performance of this specification. However, we checked that this is due to the shorter

²⁰ Additionally, one period lagged variables are used to mitigate potential endogeneity issues. Indeed, contemporaneous variables may not be exogenous if the effects of the banking crisis propagate quickly to the rest of the economy (Demirgüç-Kunt and Detragiache, 1998).

²¹ The AUROC is calculated from the ROC curve, which plots the combinations of true positive and false positive rates attained by the model. It corresponds to the probability that a classifier ranks a positive instance higher than a negative one. The AUROC ranges from 0.5 to 1, where 0.5 corresponds to the AUROC of a random classifier, while 1 that of a perfect classifier. The closer the AUC is to one, the better the model predicts.

period of analysis, namely from 1992 to 2017, rather than deriving from the inclusion of the VIX among the set of regressors.

Turning to emerging economies (**Table 8**), the probability of the occurrence of a crisis is positively associated to higher levels of inflation, while it is negatively related to higher levels of public debt and, albeit mildly, current account deficits (**Column 1**). Yet, external debt does not meaningfully affect the probability of experiencing a crisis episode. As for the global variables, only the 10y US Treasury rate is significantly related to the likelihood of observing a crisis. This suggests that vulnerabilities in emerging countries cannot be detected through changes in world GDP growth, as they are less open economies.

TABLE 8 ABOUT HERE

When we consider the specification where the outcome variable identifies pre-crisis periods (**Column 2**), inflation loses its statistical relevance, although the associated coefficient is still positive. These results are confirmed when we drop observations corresponding to the post-crisis periods and, as expected, the predictive power of the model increases (**Column 3**). When we include the interaction between the 10y US Treasury rate and the external debt in Equation (1), this term positively affects the likelihood of observing a pre-crisis period and the external debt gains significance with a negative sign (**Column 4**). Our last specification confirms that the VIX cannot be interpreted as a leading indicator of banking crisis, as suggested by the negative sign of its coefficient (**Column 5**). Also, we recover further evidence that limiting the analysis to the post-1992 period increases the predictive power of the model.

All in all, our findings are in line with those of similar work.²² Richter et al.'s (2017) analysis of banking crises for a sample of 17 developed economies find a positive, although insignificant, coefficient associated with credit-to-GDP. They also find that current account deficits increase the probability of observing a crisis. In Caggiano et al. (2014), banking crises events in Sub-Saharan African countries are not significantly related to inflation. As regards world GDP growth, we reconcile the observed positive coefficient with findings from Kaminsky and Reinhart (1999) that output tends to peak about 8 months before the onset of a crisis.²³

5.2 The predictive performance of logit models

To evaluate the predictive performance of the logit model, we split each of our subsamples into a *training* and a *testing* set. The training set is used to estimate the model and the testing set to assess how well the model fits the data. More specifically, we build our training set by randomly picking 80% of the observations. We use the training set to estimate Equation (1). From this first step we compute predicted probabilities of observing a crisis or a pre-crisis period for country *i* at time *t*. The second step consists of applying these probabilities to the remaining 20% of observations to test our model's predictions.²⁴ We replicate this procedure 1,000 times.

²² Results hold when we include real GDP growth rates at the country level in the set of regressors. See **Table B1** and **B2** in the Appendix for the corresponding marginal effects.

²³ They refer to countries' GDP growth, which determines world GDP growth.

²⁴ For our preferred specification (Column 3 of **Table 7** and **Table 8**) in each draw, the training set comprises 762 and 1,608 observations for the sample of advanced and emerging economies, respectively. Consequently, the testing set includes 191 and 402 observations for the sample of advanced and emerging economies, respectively. Worthy of note is that the number of observations for the training and the testing will always be the same across each of the 1,000 replications although not necessarily identical.

From each replication, we calculate various performance indicators typically used to assess the goodness of fit of any classification model, including machine learning algorithms: ROC and associated AUROC (see Section 5.1), accuracy, precision and sensitivity rates. Accuracy, precision and sensitivity rates derive from the so-called "confusion matrix", which compares predicted values with observed ones (**Table 9**). Accuracy is defined as the ratio between the observations correctly predicted and total observations, while precision is the ratio between the correctly predicted 1s and total predicted 1s. Sensitivity is the ratio between the correctly predicted 1s and total observed 1s.

TABLE 9 ABOUT HERE

Performance indicators can be computed both for the training set and for the testing set. In the former case the evaluation is in-sample, while in the latter is out-of-sample. In the following, we only comment on the out-of-sample performance of our preferred specification of Equation (1), i.e. the one corresponding to Column (3) of **Table 7** and **8**.²⁵ As we perform 1,000 replications, and thus have 1,000 possible realisations, we need to summarize our results in the most convenient fashion.

Starting from the predicted probabilities, we take the average of the predicted probabilities calculated in each replication by country and year. We then plot the yearly distribution of these averaged probabilities in panel (a) of **Figure 2** and **Figure 3** for the subsample of advanced and emerging economies, respectively. For ease of comparison, panel (b) of each figure shows the number of precrises actually observed in our dataset. Some additional comments follow. For advanced economies (**Figure 2**), the estimated probabilities are a good predictor of banking crises. They increase in the run up to the most widespread and severe crises, notably those of the beginning of the 1990s and of 2008. Also, they perform relatively well for the patchier crises, such as those of the early 80s. Turning to emerging economies (**Figure 3**), the fitted probabilities perform well for the cluster of crises concentrated at the beginning of the 80s. Yet, their performance is rather poor with regards to the banking crises of the 90s. A possible reason is that the model, and more specifically the set of explanatory variables, chosen is not the most suitable to detect this group of banking crises.

FIGURE 2 and 3 ABOUT HERE

Turning to the performance indicators, **Table 10** provides summary statistics of the distribution of the AUROC, accuracy, precision and sensitivity rates for the subsamples of advanced and emerging economies. Worth mentioning is that these indicators have been calculated after classifying each observation as a positive ("1" or pre-crisis year) or negative ("0" normal times) outcome according to the associated predicted probabilities. For classification, we have to choose a cutoff, i.e. a threshold above which observations are classified as 1 and 0 otherwise. In this exercise, and in line with the ML exercise below, we choose a cutoff equal to 0.5.²⁶

For advanced economies (**Table 10**), the AUROC is, on average, lower than the one resulting from the estimation of Equation (1) on the full sample (0.74 versus 0.80, see bottom of **Table 7**). The same observation applies to the sample of emerging economies (**Table 10**). The accuracy rate is very high for both country groups. It tells us that, on average, the model correctly predicts 8 and 9 observations out of 10 total observations for the sample of advanced and emerging economies, respectively. However, accuracy rates can be misleading especially when there is a large class imbalance problem, in our case a high number of observed 0s compared to 1s. When the sample is unbalanced, the model

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²⁵ In-sample performance indicators are available from the authors upon request.

²⁶ We choose a cutoff of 0.5 to make the results from the logit model comparable to those obtained when employing the AdaBoost. Another approach we use is to employ a cutoff equal to the mean of the predicted probabilities conditional on the true outcome being 1. These results are available from the authors upon request.

is correctly predicting the majority class and thus, achieving a high classification accuracy. For this reason, accuracy rates can be a poor measure of the model's performance and additional measures, such as precision and sensitivity are required to evaluate the classifier.

The precision rate for advanced economies (**Table 10**) suggests that, on average, the model correctly predicts almost 7 out of 10 predicted pre-crisis episodes. Yet, the sensitivity rate implies that the model correctly predicts only 2 out of 10 observed pre-crisis episodes. Turning to emerging economies, the model performs rather weakly. According to the precision rate, the model on average correctly predicts 3 out of 10 predicted pre-crisis episodes. The sensitivity rate suggests that the model predicts less than 1 out of 10 observed pre-crisis episodes.

TABLE 10 ABOUT HERE

Finally, **Figure 4** plots the ROC curves for the subsample of advanced – panel (a) – and emerging economies – panel (b). In particular, from the 1,000 ROCs obtained, for each country group we choose the one with a value of the AUROC nearest to the mean shown in **Table 10**. The AUROC corresponding to the chosen ROCs is 0.74 and 0.75 for advanced and emerging economies, respectively.

FIGURE 4 ABOUT HERE

6. Supervised machine learning: Decision tree classifiers

Economists are increasingly employing supervised machine learning in empirical works where the main objective is to perform predictions and where it is necessary to extrapolate information from large datasets characterized by high heterogeneity (see Athey, 2018, for an overview). With reference to the crises literature, examples in this direction are Manasse and Roubini (2009) for sovereign debt crises, and Duttagupta and Cashin (2011) and Alessi and Detken (2018) for banking crises.

Before moving to the novel empirical application of our paper, we shortly introduce machine learning and decision tree classifiers. According to Athey (2018), the field of ML is concerned with the development of algorithms suitable to be applied to large and heterogeneous datasets, with the main objectives being prediction, classification and clustering. ML is of two types, supervised and unsupervised. Unsupervised ML infers patterns from a dataset without reference to known or labelled outcomes. It can be applied to clustering (i.e. splitting the dataset into groups according to similarity) or dimensionality reduction (i.e. reducing the number of features in a dataset). Instead, supervised machine learning is suitable for a wide range of applications where the aim of the analysis is to predict an outcome based on the behaviour of a set of predictors or "features" (the equivalent of covariates or explanatory variables in econometrics). In other words, it revolves around the problem of prediction (Kleinberg et al., 2015; Mullainathan and Spiess, 2017). Here, we focus on supervised machine learning.

In this paper, we have a dataset that includes a binary outcome variable (pre-crisis vs normal times, see Section 3) and a set of features (see Section 4). We wish to perform out-of-sample forecasts to predict the likelihood that a banking crisis may occur within a three-year spell. We are dealing with a prediction problem, which fits within the framework of supervised machine learning. The most straightforward way to address the issue is to apply a logistic regression (as in Section 5). However, the ML literature suggests the use of alternative nonlinear methods that are concerned primarily with prediction, unlike traditional econometric methods, which are not optimised to solve prediction

problems (Kleinberg et al., 2015).²⁷ Examples of supervised ML methods are Classification and Regression Trees (CART), Random Forests (RF) and Adaptive Boosting (AdaBoost).²⁸

In our empirical exercise, we address what in machine learning terminology is called a *classification problem*. A way to solve it is to use a *decision tree classifier*. The simplest classifier is CART, while more complex ones (the so-called *ensemble models*) are RF and AdaBoost.²⁹ Broadly speaking, these methods select features – and their critical values – to classify the outcome variable. They offer some advantages. First, they are particularly appropriate when datasets are large and characterised by high heterogeneity. Second, they have the ability to capture non-linear relationships and to identify relevant interactions among two or more variables. Third, they are not sensitive to missing values – they replace them with the most probable value – or to outliers. Finally, they allow a large explanatory set, since the statistical algorithm is able to select the most relevant variables in predicting the outcome. Before applying a decision tree classifier, the dataset is conventionally split into a *training* and a *testing set*: the training set is used to estimate ("train") the model (or "tree") and the testing set to evaluate the predictive performance of the model.

Specifically, a decision tree classifier is a partitioning algorithm that recursively chooses the predictors and the thresholds that are able to best split the sample into the relevant classes (in our case, precrisis and normal times) according to a so-called "impurity measure". Technically, the tree starts from a *root node*, which collects all the training set observations. The initial sample is split into two *child nodes*, according to one of the aforementioned impurity criteria. Each of these child nodes can be further divided into two more child nodes based on the variable that best splits the corresponding subsamples. This recursive procedure stops when there is no further gain in splitting a subset (i.e. the impurity measure does not improve) or a binding rule applies (i.e. the pre-set maximum number of splits has been reached). The nodes that cannot be optimally split further are called *terminal nodes*. **Figure A1** in Appendix A depicts an example of classification tree.

These models may suffer from two drawbacks: instability and overfitting. Instability implies that small changes in the training set may cause large changes in classification rules. For instance, we could obtain two different trees from two similar training samples if the algorithm does not select the same variable in the first split. Overfitting refers to the tree's generalisation capability: an overfitted model gives a highly accurate prediction in sample, but a poorly accurate one out of sample. This could happen when too many splitting rules are applied compared to data availability.

Ensemble models, such as random forests and adaptive boosting, seek to overcome these limitations. As regards instability, these algorithms train many decision trees on different subsamples ("folds") of the initial dataset and then combine them in order to give a final prediction. As regards overfitting, it can be avoided by correctly setting some parameters ("regularizers", see below).

Both RF and AdaBoost estimate a multitude of trees to grow a forest, allowing us to obtain a strong and stable model from many weak and unstable ones. However, they differ in how they aggregate

²⁷ The empirical economic literature (e.g. Manasse and Roubini, 2009, Duttagupta and Cashin, 2011, and Alessi and Detken, 2018) benchmarks ML results against those of logit models.

²⁸ Other supervised ML techniques include penalised regression (e.g. LASSO and elastic nets), support vector machines (SVM), neural nets and matrix factorisation (for further details, see Varian, 2014, and Athey, 2018).

²⁹ See Freund and Schapire (1996) on Adaptive Boosting.

³⁰ Given the distribution of a discrete variable contained in a node, we define impurity a measure of its dispersion. In each node, the choice of the predictor and of the cut-off point is made in order to maximize the reduction of impurity from the parent node to its child nodes. Examples of impurity measures are the Gini index and entropy.

trees to get a final overall result. On the one hand, RF randomly resamples the training set and estimates N single models in parallel. It subsequently averages across models in order to improve the performance of the estimator ("bagging"). On the other hand, AdaBoost builds N base models sequentially where misclassified observations are attributed a higher weight in each replication ("boosting"). Both algorithms perform better than CART, but the interpretation of their outcome is less intuitive since no final tree is represented: we can compare the importance of the variables but not the way they interact.

Their implementation requires pre-setting the regularizers: (i) *tree depth*, i.e. maximum number of nodes along the longest path from the root note down to the farthest leaf node; (ii) *minimum split*, i.e. minimum number of observations in a node to allow for a split; and (iii) *number of final trees*, i.e. number of trees (base models) in the forest. In addition, AdaBoost involves choosing the function that attributes increasing weight to the incorrectly classified observations at each round. Since AdaBoost corrects for misclassified observations and its predictive power is higher, we rely on it for the empirical analysis of Section 7.

7. The results from classification trees

In this section, we preliminarily clarify some technical issues concerning the AdaBoost implementation and, then, we present the main results of our analysis, which aims at assigning a probability to the event that a country is involved in financial troubles over a three-year horizon. For this purpose, our outcome variable is the one that classifies the "pre-crisis" years as 1 and normal times as 0. As discussed in Section 3, pre-crisis spells correspond to the three years preceding a banking crisis. In order to avoid the post-crisis bias, we drop the observations corresponding to three years following a crisis (the post-crisis years), so that the 0s mark normal times only. Therefore, our outcome variable is what we labelled definition 2b in **Table 4** of Section 3. Moreover, we exclude all observations for which one or more variables are not available: our full sample is the same as that of the logit specification, i.e. 953 observations for the advanced economies and 2,010 observations for the emerging ones.

The analysis is performed separately on the two sub-samples of advanced and emerging economies. The rationale for applying the algorithm to the two subsamples separately is to take into account any differences in model parameterization and variable selection.

7.1 Model specification: variables and parameters

As introduced in Section 4, the variable set is split into two groups, country-specific and global. The country-specific variables are of two types, ratios and rates (**Table A3**). The analysis is performed on two sets of variables: (i) one that corresponds to the one employed in the logit model and (ii) an enlarged one that includes two additional sets of variables. These two additional sets are composed of the detrended and standardized transformations of the country-specific variables expressed as ratios (with the exception of the the current account to GDP, which is already standardised).

First of all, we need to be careful in avoiding overfitting. Indeed, an overfitted model could have a low out-of-sample predictive power because of its over-adaptation to the training sample. Likewise, neither an under-fitted model is suitable. From this perspective, the parameter setting appears crucial in this framework. To choose the best combination, we build a simple objective function based on four elements:

$$U(\cdot) = \beta_1 PREC_{OUT} + \beta_2 SENS_{OUT} - \beta_3 (PREC_{IN} - PREC_{OUT}) - \beta_4 (SENS_{IN} - SENS_{OUT})$$
 (2)

where PREC and SENS represent precision and sensitivity, respectively. According to Equation (2), the objective function depends on the out of sample precision and sensitivity and on the difference between the in-sample and out-of-sample levels of these measures. The initial preference set (β s) is equal to (0.4, 0.4, 0.1, 0.1) in order to maximize the efficiency of the algorithm and to take into account at the same time the overfitting issue. On the one hand, the inclusion of the two individual indicators aims at identifying a great proportion of crisis episodes (SENS) without making too many mistakes, especially false alarms (PREC). On the other hand, the differences between the in-sample and the out-of-sample performance with reference to the two indicators are useful to prevent the setting of the parameters from generating overfitting. We perform a grid search over our three main regularizers: maximum depth of each tree, the number of trees and the minimum number of observations in each node.

Figure 5 shows the values assumed by our objective function in correspondence of each combination of the three parameters.³² The objective function is at its maximum when the model is trained with maximum depth, number of trees and minimum split set at 3, 35 and 70 for advanced economies and the parameter set (4, 35, 30) for emerging countries. This result holds when using several random training datasets and different preference sets.

FIGURE 5 ABOUT HERE

7.2 Model performance indicators

The analysis of this section is carried out on the two subsamples of advanced and emerging economies. The performance of the model is assessed in terms of standard measures of model precision, i.e. sensitivity, accuracy and AUROC.

Initially, we exactly replicate the analysis performed by means of the logit model. In analogy to Section 5, the sample is divided into a training and a testing set: the former consists of 80% of the sample randomly selected and is used to train the model, the latter contains the residual 20% and it is employed to assess the out-of-sample performance of the model. We perform 1,000 replications of this procedure and we calculate the performance indicators for each replication.

Table 11 shows the mean, median and standard deviation of the distributions of out-of-sample sensitivity, precision, accuracy and AUROC for both advanced and emerging economies. As in the logit model, the threshold above which observations are classified as 1 is 0.5. For advanced economies, the sensitivity rate is equal to 0.36, i.e. on average almost 4 out of 10 observed pre-crises are identified, while a lower sensitivity is recorded for emerging countries (0.13). The precision rate tells us that when the predicted value is equal to 1, the model classifies observations correctly almost 7 times out of 10 (0.68) for advanced countries and 3 times out of 10 (0.34) for emerging economies. The accuracy rate is around 0.9 for both country groups, but as we already warned in Section 5, we must use caution in interpreting this measure since we are working with a strongly unbalanced outcome variable with respect to the relative weight of 1s. Finally, the AUROC shows a good performance for both country groups, with a value of 0.85 for advanced countries and 0.82 for emerging ones.

TABLE 11 ABOUT HERE

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³¹ Accuracy and sensitivity lie between 0 and 1, so that their square values are smaller. In this way, we want to reduce the contribution of these factors to the objective function.

³² The maximum depth and the Minimum split can be read along the X and Y axis, respectively. The bar height describes refers to the maximum depth.

Having established that AdaBoost outperforms the logit model, we further test its predictive performance by including an additional transformation (i.e. standardisation) of the country-specific variables (with the exception of the current account to GDP, which is already standardised in our base models) in the variables set. Regarding the advanced economies, (Table 12) the out-of-sample performance shows an AUROC of 87%, a precision of 75% and a sensitivity of 43%. Worthy of note is that in this specification the misclassified observations are mainly "missed pre-crisis", while only a low number of "false alarms" is issued. Conversely, for the subsample of emerging economies, the values of the accuracy rate is the same as that for the advanced economies, but out-of-sample sensitivity and precision are lower, 16% and 46%, respectively.

TABLE 12 ABOUT HERE

Although sensitivity and accuracy rates are two valid and commonly used measures to evaluate the predictive capacity of a binary classification problem, they are not independent of the threshold used to discriminate between 0s and 1s. For this purpose, we refer to the ROC Curve and to the area below it (AUROC).33 Concerning advanced economies, the model performance appears satisfactory, as AUROC equals 0.876 (Table 12). A slightly decline in the AUROC is recorded if we consider the emerging economies (0.841), coherently with the results obtained for the other performance measures.

Finally, we discuss the relevance of the variables included in the analysis. As already argued in Section 6, ensemble methods (e.g. random forest and AdaBoost) do not return a single final tree and, hence, nothing can be said on how the variables interact. Moreover, the algorithm does not provide information about how and how much these variables affect the probability of a pre-crisis, so that we can only rank them according to their importance.

Figure 6 shows the ranking of the ten most important variables for our two sets of countries. For the advanced countries, the global variables US 10y rate and world growth are among the most important ones (1st and 4th place, respectively), possibly indicating the relevance of external conditions in triggering a crisis. Banking variables display a higher importance as standardised credit-to-GDP and credit to deposits ratio are 2nd and 5th, while both detrended and standardised public debt are also important. Results about emerging economies confirm the importance of US monetary policy to the outbreak of the banking crises as well as the banking variables. As we expected, the importance of inflation and current account represents a novelty with respect to advanced countries.

FIGURE 6 ABOUT HERE

7.3 Out-of-sample exercise and prediction

Since the goal of this paper is to develop an early warning system for banking crises, we perform a forecasting exercise on both advanced and emerging economies from 1990 to 2017. Specifically, we start by training the models on the subsample 1970-1989 to make predictions in 1990 and compare the predicted values with the observed ones. By doing so, we are able to detect whether an observation is correctly predicted and, if not, we are able to distinguish between a "missed crisis" and a "false alarm". We recursively repeat the same exercise from 1991 to 2017 by adding a new year to the training sample at each round and testing it on the first excluded year. Results are depicted in

³³ The AUROC is calculated from the ROC curve, which plots the combinations of true positive and false positive rates attained by the model. It corresponds to the probability that a classifier ranks a positive instance higher than a negative one. The AUROC ranges from 0.5 to 1, where 0.5 corresponds to the AUROC of a random classifier, while 1 that of a perfect classifier. The closer the AUC is to one, the better the model predicts.

Figure 7: for advanced economies the model shows a good ability in learning from the past as the closer the crisis year, the greater the number of pre-crisis identified. In 2005, the first pre-crisis year for many countries, the model has a modest predictive performance, likely related to the fact that data are not informative because of their proximity to normal times. In 2006 and 2007, more crises are correctly predicted because the model exploits the information on 2005. That is not true for the emerging economies, for which only few pre-crisis episodes are signalled by the model over the prediction horizon. On the other side, in both models the number of false alarms is limited. Moreover, these predicted false alarms do not necessarily signal a false crisis because it is possible that policy makers/monetary institutions enforced policies aimed at preventing the potential banking crisis. Obviously, no machine learning method (as no other model) can account for this.

FIGURE 7 ABOUT HERE

A different way to look into our results is to focus on the probability distributions over time retrieved from the AdaBoost for the two groups of countries. In **Figure 8**, we represent for both sub-samples the maximum and the minimum predicted probabilities as well as the median and the values corresponding to the first and the third quartiles by year.

FIGURE 8 ABOUT HERE

We can infer two main results from the probability distributions: (i) they tend to evolve quite coherently with the number of observed pre-crisis periods in both sub-samples, and (ii) they show a higher variance in pre-crisis periods than in tranquil times. These two results indicate that our predicted probabilities perform well in replicating the path of financial vulnerability across countries and in capturing the fact that in pre-crisis periods countries behave differently.

Moreover, we note an upward shift of the distributions in 2017 for the advanced economies, below the levels reached in the years preceding the 2007-2008 crisis, but closer to the levels reached during the 2011-2012 sovereign debt crisis in Europe. This increase may signal a mounting fragility for the advanced economies. By contrast, for emerging economies probabilities remain low, notwithstanding the problems occurred to some countries in the last year.

Looking at the country-specific probabilities in more detail, among the advanced countries the most vulnerable ones in 2017 Iceland, Greece, Finland, Czech Republic and Denmark: their probabilities of incurring a banking crisis over a three-year horizon ranges from 35% to 28% (**Table 13**). Conversely, emerging economies record low probabilities: the most vulnerable one is Seychelles (21%), followed by Paraguay (19%), Hungary (19%), Croatia (17%) and Azerbaijan (17%).

Coming back to the advanced countries, Germany, Austria, Japan, France and Latvia turn out to be the less exposed to financial risks, with a probability between 10% and 17%. Among the emerging economies, Philippines, Ecuador, Morocco, Thailand and Indonesia result the less vulnerable (less than 5%).

In 2006, in the build-up of the financial crisis, Spain, Estonia, Iceland, Denmark, Portugal were the most fragile countries, with probabilities ranging between 54% for Luxembourg and 58% for Iceland, far higher than actual probabilities. For emerging economies probabilities were lower, consistent with the lower number of observed crises. The most exposed countries were Syria, Romania, Ukraine, South Africa and Croatia.

TABLE 13 ABOUT HERE

For both models, a graphical illustration of the comparison between 2006 and 2017 predicted probabilities by means of heat maps is presented in **Figure 9**, where darker colours correspond to higher probabilities to be in a pre-crisis year.

FIGURE 9 ABOUT HERE

7.4 A comparison with the logit model

The predictive performance of the logit model and that of the AdaBoost can be compared in terms of AUROC, precision, sensitivity and accuracy rates. We have already commented upon their performances separately in Section 5.2 (**Table 10**) and Section 7.2 (**Table 11**). Herein we wish to put side by side the main results of both models.

Overall, the AdaBoost outperforms the logit. Specifically, the AdaBoost delivers a better out of sample performance than the logit model in terms of AUROC, especially for advanced economies (0.846 vs 0.74). The corresponding values for emerging countries are 0.815 and 0.780 for AdaBoost and logit, respectively.

The AdaBoost performs better than the logit model even when looking at the precision and sensitivity rates. As for the precision rate, the AdaBoost correctly predicts almost 7 pre-crisis events out of 10 predicted pre-crises in advanced economies, but only 3 out of 10 for the sub-sample of emerging economies. The logit model delivers a similar precision rate for advanced countries, but an even lower one for emerging countries. In terms of sensitivity, the AdaBoost correctly predicts almost 4 pre-crises out of 10 observed pre-crisis events for advanced economies, but only 1 in emerging economies. The logit model delivers lower sensitivity rates for both country groups. Finally, when we enlarge the variables set, the AdaBoost improves its performance in terms of all indicators.

8. Concluding remarks

The dramatic worldwide losses triggered by the 2007-2008 financial crisis urged policy makers to understand the macroeconomic vulnerabilities that led to its build-up. In particular, as the crisis spread as a systemic banking crisis, the connections between money and credit fluctuations and financial crises took centre stage. The ultimate goal was to layout macroprudential policies that could warrant a timely response to countries' weaknesses, thereby significantly limiting the burdensome costs entailed by similar crises.

Economists have responded to this appeal by developing EWSs aimed at detecting the risks that a systemic banking crisis may arise. This literature has evolved along different lines, from the signals approach, to discrete choice models to machine learning. These contributions build on, and partially overlap with, a wide field of research directed at characterising banking crises episodes according to a range of criteria.

With this paper, we contribute to the existing literature by developing an EWS to predict the build-up of banking crises in both advanced and emerging economies. To this end, we use an integrated dataset of banking crises and macroeconomic indicators that includes 100 countries (33 advanced and 67 emerging) spanning from 1970 to 2017. We develop an EWS by using both a supervised machine learning algorithm, namely Adaptive Boosting (AdaBoost), and traditional econometrics, namely the logit model. We wish to combine the output from both methodologies to provide the necessary tools to predict the build-up of a banking crisis.

Both models entail pros and cons. Ease of use and interpretation are the main advantages of the logit model together with the possibility of assessing the statistical relationship between the single indicator and the probability of observing a pre-crisis event. An advantage of AdaBoost lies in its ability to capture non-parametric relationships.

Overall, the AdaBoost shows a higher predictive performance than the logit model. Both models deliver increasing predicted probabilities in the last years of the sample, warning against the possible build-up of pre-crisis macroeconomic imbalances.

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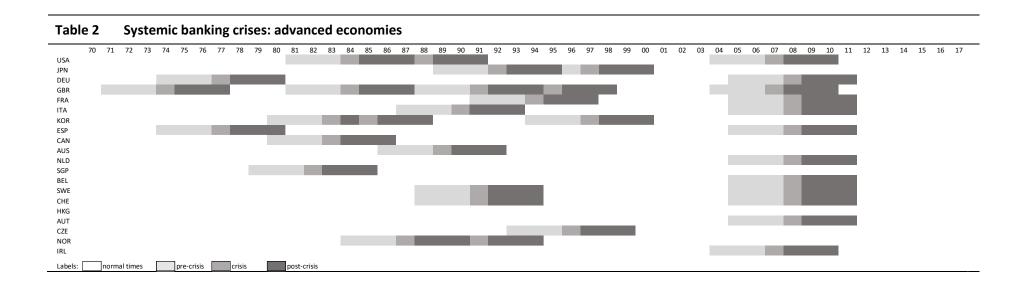
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TABLES

Table 1	Definition of sub-periods
Pre-crisis	up to 3 years prior to the crisis
Post-crisis	up to 3 years after the crisis
Normal tim	no crisis in the preceding 3 years and no crisis in the subsequent 3 years



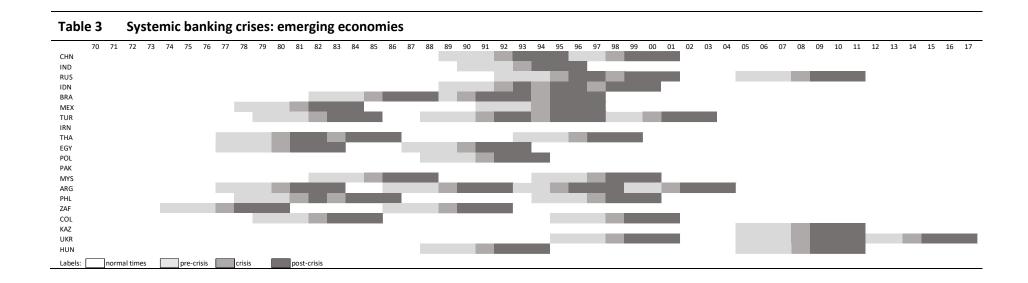


Table 4 De	finitions of the target variable	
	Target variable = 1	Target variable = 0
Approach 1 Approach 2	crisis	Normal times + pre-crisis + post-crisis
(a)	pre-crisis	Normal times + post-crisis
(b)	pre-crisis	Normal times

In definition 2a, crisis episodes are dropped from the dataset.

In definition 2b, crisis and post-crisis episodes are dropped from the dataset.

Table 5 Summary statistics (mean values)

	Ove	erall	Norma	l times	Pre-	crisis	Cri	sis	Post-	crisis	
	Advanced	Emerging	No. Obs.								
Country-specific											
Current Account-to-GDP	-0.02	-1.52	0.41	-1.43	-1.69	-2.18	-2.08	-2.44	-0.58	-1.42	3955
External Debt-to-GNI	164.29	45.70	149.21	43.40	202.94	48.56	205.20	53.31	213.81	60.46	3977
Public Debt-to-GDP	53.51	48.43	53.71	47.25	47.46	49.75	49.56	53.05	58.73	56.35	4078
Inflation	6.04	50.56	6.13	26.91	6.41	104.33	6.12	195.73	5.07	167.56	4159
Real effective Exchange Rate	0.36	0.75	0.46	0.94	0.77	1.03	1.27	-0.74	-0.91	-0.28	2302
Openness Index	92.77	76.95	97.29	79.28	79.85	68.76	77.58	64.85	78.24	67.86	4150
Credit-to-GDP	124.41	39.36	120.92	39.45	128.58	38.50	136.64	42.83	140.24	38.11	3964
Bank Credit-to-Bank Deposits	112.49	94.55	106.73	91.77	128.15	106.55	131.06	107.39	129.37	104.95	4088
House price	2.77	2.09	3.34	2.84	5.71	6.18	-1.78	-0.96	-2.13	-4.89	1823
Global											
10y US Treasury Rate	6.48	6.48	6.47	6.26	7.15	7.82	6.61	7.81	5.91	7.20	4800
Energy price Index	8.35	8.35	9.01	9.10	10.58	7.33	9.22	2.31	1.21	3.69	4700
Real World GDP growth	3.14	3.14	3.20	3.19	3.39	3.09	2.65	2.66	2.61	2.84	4800
VIX average	19.37	19.37	19.23	19.49	15.44	17.40	23.20	19.68	21.81	19.51	2800
VIX max	33.23	33.23	32.36	33.91	24.99	27.18	49.05	33.80	39.01	31.24	2800
Detrended and normalized											
Current Account-to-GDP	0.00	0.00	0.07	0.00	-0.21	-0.15	-0.60	-0.17	-0.05	0.16	3955
External Debt-to-GDP	0.00	0.00	-0.11	-0.02	0.28	-0.25	0.27	0.10	0.37	0.38	3977
Public Debt-to-GDP	0.00	0.00	0.08	0.00	-0.61	-0.39	-0.71	0.00	0.25	0.29	4078
Openness Index	0.00	0.00	0.03	0.00	0.17	-0.02	0.04	-0.07	-0.34	0.07	4150
Credit-to-GDP	0.00	0.00	-0.15	-0.04	0.24	0.20	0.68	0.76	0.60	-0.03	3964
Bank Credit-to-Bank Deposits,	0.00	0.00	-0.11	-0.03	0.21	0.17	0.56	0.39	0.31	-0.03	4088
10y US Treasury Rate	0.00	0.00	-0.01	-0.01	0.30	-0.11	0.02	0.26	-0.18	0.11	4800

Source: Authors' own elaborations based on BIS, CBOE, IMF and WB.

Table 6 T-test on full sample averages

	1	
	Difference	t-stat
Current Account-to-GDP	1.50***	4.3
Public Debt-to-GDP	5.07***	4.2
External Debt-to-GNI	118.58***	11.8
Inflation	-44.52***	-4.1
Real effective Exchange Rate	0.00	-0.9
Openness Index	15.82***	8.5
Credit-to-GDP	85.04***	30.5
Bank Credit-to-Bank Deposits	17.94***	11.5
House price	0.69	1.2

Note: This table presents tests of differences in the means presented in **Table 5**.

* p<0.05; ** p<0.01; ***p<0.001.

Source: Authors' own elaborations based on BIS, CBOE, IMF and WB.

	(1)	(2)	(3)	(4)	(5)
	crisis	precrisis (2a)	precrisis (2b)	precrisis (2b)	precrisis (2b)
					1992-2017
Current account-to-GDP	0.003	-0.004	-0.000	-0.000	-0.006
	(0.006)	(0.013)	(0.015)	(0.015)	(0.0156)
External debt-to-GNI	0.027***	0.036***	0.048***	0.048	0.054***
	(0.003)	(0.009)	(0.012)	(0.030)	(0.011)
Public debt-to-GDP	-0.034***	-0.090***	-0.095***	-0.095***	-0.092***
	(0.007)	(0.014)	(0.016)	(0.016)	(0.019)
Credit-to-GDP	0.010**	0.004	0.018	0.018	0.032*
	(0.005)	(0.013)	(0.015)	(0.015)	(0.017)
10y US Treasury rate	0.006***	0.011**	0.011*	0.011**	0.052***
	(0.002)	(0.005)	(0.006)	(0.005)	(0.016)
Real world GDP growth	0.012***	0.024***	0.022***	0.022***	0.079***
	(0.003)	(0.007)	(0.008)	(0.007)	(0.014)
External debt-to-GNI*US 10y Treasury rate				0.000	
				(0.005)	
VIX max					-0.015***
					(0.002)
Country dummies	YES	YES	YES	YES	YES
No. obs.	1,120	1,098	953	953	497
Pseudo R-squared	0.244	0.199	0.223	0.223	0.537
AUROC	0.845	0.795	0.802	0.801	0.947

Note: In Column (1) crisis = 1 identifies the year when the crisis occurs, 0 otherwise, and the set of explanatory variables are taken at t-1. In Column (2) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise. In Columns (3)-(5) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise except post-crisis years. From Columns (2) to (5) explanatory variables are taken at time t. All variables are detrended and standardised, with the exception of Current account-to-GDP (only standardised), 10y US Treasury rate, Real world GDP growth and VIX max. In Column (5) the logit is applied to data as of 1992 since the VIX is only available from that date forward. The AUROC is the area under receiving operating characteristic. Standard errors in brackets are clustered at the country level. * p < 0.05; ** p < 0.01; ***p < 0.001.

Table 8 Marginal effects: Emerging	economies	s, 1970-2017			
	(1)	(2)	(3)	(4)	(5)
	crisis	precrisis (2a)	precrisis (2b)	precrisis (2b)	precrisis (2b)
					1992-2017
Current account-to-GDP	-0.007*	-0.010	-0.009	-0.010	-0.024***
	(0.004)	(0.009)	(0.011)	(0.010)	(0.009)
External debt-to-GNI	-0.000	-0.009	-0.003	-0.054***	-0.013
	(0.007)	(0.013)	(0.015)	(0.020)	(0.014)
Public debt-to-GDP	-0.016**	-0.026*	-0.029**	-0.033**	-0.032**
	(0.007)	(0.013)	(0.015)	(0.015)	(0.013)
Inflation	0.000**	0.000	0.000	0.000	0.000
	(0.000)	(0.000)	(0.000)	(0.000)	(0.000)
10y US Treasury rate	0.006***	0.015***	0.020***	0.022***	0.038***
	(0.001)	(0.002)	(0.003)	(0.003)	(0.006)
Real world GDP growth	0.001	0.006	0.004	0.003	-0.007
	(0.003)	(0.004)	(0.004)	(0.004)	(0.006)
External debt-to-GNI*US 10y Treasury rate				0.007***	
				(0.002)	
VIX max					-0.002***
					(0.001)
Region dummies	YES	YES	YES	YES	YES
No. obs.	2,273	2,244	2,010	2,010	1,292
Pseudo R-squared	0.125	0.130	0.159	0.167	0.352
AUROC	0.794	0.785	0.803	0.808	0.915

Note: In Column (1) crisis = 1 identifies the year when the crisis occurs, 0 otherwise, and the set of explanatory variables are taken at t-1. In Column (2) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise. In Columns (3)-(5) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise except post-crisis years. From Columns (2) to (5) explanatory variables are taken at time t. All variables are detrended and standardised, with the exception of Current account-to-GDP (only standardised), Inflation, 10y US Treasury rate, Real world GDP growth and VIX max. In Column (5) the logit is applied to data as of 1992 since the VIX is only available from that date forward. The AUROC is the area under receiving operating characteristic. Standard errors in brackets are clustered at the region level. * p<0.05; ** p<0.01; ***p<0.001.

Table	9	Confu	sion matrix	
		Obse O	erved	- Accuracy = $\frac{a_{00} + a_{11}}{a_{00} + a_{01} + a_{10} + a_{11}}$
		U		$a_{00} + a_{01} + a_{10} + a_{11}$
cted	0	a_{00}	<i>a</i> ₀₁	- Sensitivity (or True positive rate) = $\frac{a_{11}}{a_{01} + a_{11}}$
Predicted	1	a_{10}	a_{11}	- Precision = $\frac{a_{11}}{a_{10} + a_{11}}$

Table 10 Logit model: Out of sample performance

(a) advance	d economies	5	(1	b) emergir	ng economie:	5
	Mean	Median	Std. Dev.		Mean	Median	Std. Dev.
Sensitivity	0.226	0.222	0.077	Sensitivity	0.044	0.043	0.030
Precision	0.680	0.667	0.173	Precision	0.334	0.333	0.230
Accuracy	0.883	0.885	0.021	Accuracy	0.903	0.903	0.013
Auroc	0.74	0.74	0.050	Auroc	0.780	0.780	0.030

Note: Summary statistics of performance indicators on a total of 1,000 replications. Each AUROC is derived from estimating the logit model in Column (3) of **Table 7**. Precision, Sensitivity and Accuracy rates are calculated from 1,000 confusion matrices where the cutoff employed to classify the 191 out-of-sample observations is equal to 0.5.

Source: Authors' own elaborations

Note: Summary statistics of performance indicators on a total of 1,000 replications. Each AUROC is derived from estimating the logit model in Column (3) of **Table 8**. Precision, Sensitivity and Accuracy rates are calculated from 1,000 confusion matrices where the cutoff employed to classify the 402 out-of sample observations is equal to 0.5.

Table 11 AdaBoost: Out of sample performance

(a	a) advance	d economies	5	(k	o) emergin	g economies	5
	Mean	Median	Std. Dev.		Mean	Median	Std. Dev.
Sensitivity	0.361	0.356	0.096	Sensitivity	0.131	0.128	0.056
Precision	0.675	0.667	0.127	Precision	0.438	0.429	0.159
Accuracy	0.889	0.890	0.021	Accuracy	0.904	0.905	0.013
Auroc	0.846	0.847	0.038	Auroc	0.815	0.817	0.029

Source: Authors' own elaborations

Sensitivity and Accuracy rates are calculated from 1,000 confusion matrices where the cutoff employed to classify the 191 out-of-sample observations is equal to 0.5.

Source: Authors' own elaborations

Sensitivity and Accuracy rates are calculated from 1,000 confusion matrices where the cutoff employed to classify the 402 out-of sample observations is equal to 0.5.

Table 12 AdaBoost (large variables set)

(a) advance	d economies	5	(1	o) emergin	g economies	5
	Mean	Median	Std. Dev.		Mean	Median	Std. Dev
Sensitivity	0.428	0.429	0.094	Sensitivity	0.162	0.156	0.060
Precision	0.755	0.762	0.119	Precision	0.463	0.462	0.135
Accuracy	0.903	0.906	0.019	Accuracy	0.905	0.905	0.013
Auroc	0.876	0.879	0.037	Auroc	0.841	0.842	0.028

Source: Authors' own elaborations

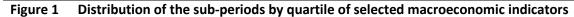
Sensitivity and Accuracy rates are calculated from 1,000 confusion matrices where the cutoff employed to classify the 191 out-of-sample observations is equal to 0.5.

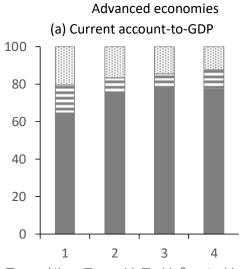
Source: Authors' own elaborations

Sensitivity and Accuracy rates are calculated from 1,000 confusion matrices where the cutoff employed to classify the 402 out-of sample observations is equal to 0.5.

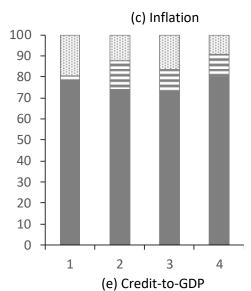
	Advance	ed economies		F	mergin	g economies		
2006	, warice	2017		2006 2017				
Spain	57.9%	Iceland	35.2%	Syria	40.7%	Seychelles	21.3%	
Estonia	57.1%	Greece	32.1%	Romania	39.6%	Paraguay	19.5%	
celand	56.5%	Finland	30.7%	Ukraine	39.5%	Hungary	19.29	
Denmark	54.7%	Czech Republic	29.6%	South Africa	38.8%	Croatia	17.39	
Portugal	54.4%	Denmark	28.3%	Croatia	38.4%	Azerbaijan	17.29	
Latvia	53.7%	Belgium	26.8%	Namibia	37.8%	Fiji	17.19	
United Kingdom	51.6%	Netherlands	26.5%	Pakistan	35.0%	Albania	17.09	
Austria	46.6%	United Kingdom	26.3%	Bosnia & Herzegovina	33.5%	Mauritius	16.49	
United States	45.2%	New Zealand	26.1%		32.5%	Romania	14.99	
New Zealand	43.6%		26.1%	Fiji Kazakhstan	32.5%	Armenia	14.99	
		Norway						
Australia	43.2%	Israel	24.3%	Jordan	32.3%	Sri Lanka	14.99	
Italy	43.0%	Luxembourg	24.1%	Barbados	29.9%	Suriname	14.49	
Canada 	39.6%	Canada	24.0%	Hungary	29.8%	Turkey	14.29	
Israel	38.8%	Ireland	23.5%	Belarus	29.4%	Poland	12.9%	
Czech Republic	38.4%	Switzerland	21.4%	El Salvador	29.0%	Bosnia & Herzegovina	12.49	
Belgium	38.3%	Hong Kong SAR	21.3%	Turkey	27.8%	Chile	12.09	
Germany	38.2%	Italy	21.1%	Algeria	27.5%	Argentina	11.89	
Ireland	38.2%	Australia	20.0%	Sri Lanka	27.1%	Belarus	11.79	
France	37.8%	Spain	20.0%	Chile	27.1%	South Africa	11.69	
Sweden	37.4%	United States	19.2%	Swaziland	27.0%	Botswana	11.59	
Greece	36.7%	Korea	18.9%	Russia	26.3%	Colombia	11.59	
Singapore	35.5%	Sweden	18.7%	Botswana	25.3%	Belize	11.49	
Slovenia	35.3%	Slovak Republic	18.5%	China	25.1%	Brazil	11.39	
Luxembourg	34.4%	Slovenia	18.4%	Costa Rica	24.9%	Panama	11.29	
Hong Kong SAR	32.6%	Lithuania	18.3%	Argentina	24.1%	Uruguay	10.79	
Netherlands	32.2%	Singapore	17.7%	Kuwait	24.1%	Malaysia	10.59	
Finland	30.8%	Latvia	17.0%	Ecuador	23.5%	Bulgaria	10.09	
Norway	29.7%	France	16.6%	India	23.2%	China	10.09	
Korea	28.0%	Japan	15.9%	Malaysia	23.1%	Mexico	9.3%	
Slovak Republic	27.9%	Austria	14.1%	Peru	22.6%	Macedonia	9.3%	
Switzerland	27.5%	Germany	9.9%	Albania	21.9%	Dominican Republic	9.2%	
Japan	20.1%	Germany	3.570	Morocco	21.8%	Guatemala	9.2%	
Јаран	20.1/0			Mexico	21.6%	Russia	9.0%	
					21.6%	Pakistan		
				Belize			8.8%	
				Georgia	21.3%	Serbia	7.6%	
				Armenia	21.0%	Egypt	7.5%	
				Poland	20.2%	Kazakhstan	6.6%	
				Indonesia	19.9%	El Salvador	6.4%	
				Jamaica	19.6%	India	6.1%	
				Thailand	18.9%	Jordan	5.9%	
				Seychelles	18.9%	Peru	5.5%	
				Suriname	18.7%	Georgia	5.5%	
				Colombia	18.5%	Costa Rica	5.0%	
				Azerbaijan	18.5%	Indonesia	4.8%	
				Gabon	17.8%	Thailand	4.0%	
				Philippines	17.0%	Morocco	4.0%	
				Angola	16.4%	Ecuador	2.6%	
				Paraguay	16.3%	Philippines	2.6%	
				Mauritius	16.0%			
				Bulgaria	16.0%			
				Tunisia	15.9%			
				Macedonia	15.1%			
				Trinidad and Tobago	13.7%			
				Venezuela	12.7%			
				Brazil	12.7%			
				Panama	11.0%			
				Egypt	11.0%			
					10.2%			
				Uruguay				
				Lebanon	8.6%			

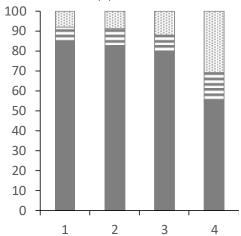
FIGURES



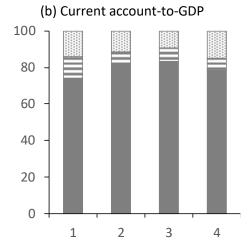




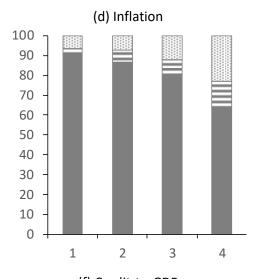




Efmeggiggeoonomiess



■ normal times ■ pre-crisis ᠍ crisis & post-crisis



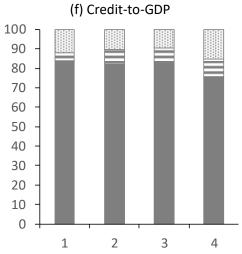
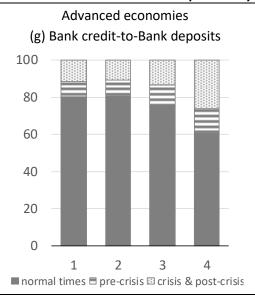
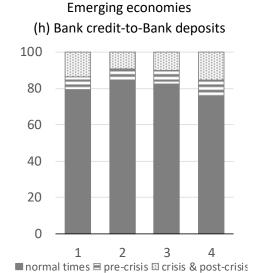


Figure 1 Distribution of the sub-periods by quartile of selected macroeconomic indicators (cont.)

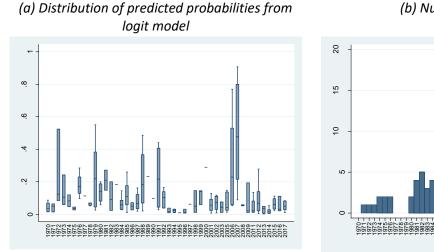


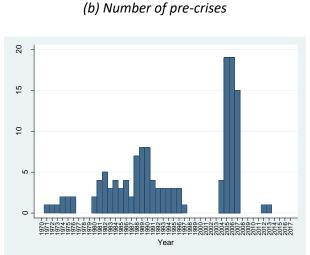


Source: Authors' own elaborations based on BIS, IMF and WB.

Note: This chart shows the distribution of the sub-periods by quartile of the selected variable. All variables are detrended and standardised except for inflation.

Figure 2 Logit model: Predicted probabilities and number of pre-crisis spells (advanced economies), 1970-2017



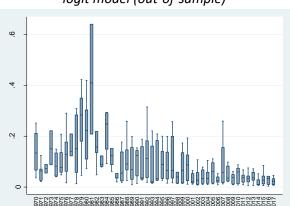


Source: Author's own elaborations

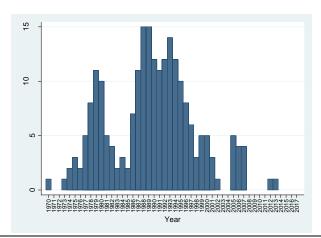
Note: Predicted probabilities shown in panel (a) correspond to the out-of-sample predictions derived from estimating the logit model in Column (3) of **Table 7** 1,000 times. Probabilities obtained from each replication are then averaged by country and year and their distribution plotted in panel (a). They are based on a total of 191 out-of-sample observations.

Figure 3 Logit model: Predicted probabilities and number of pre-crisis spells (emerging economies), 1970-2017

(a) Distribution of predicted probabilities from logit model (out-of-sample)



(b) Number of pre-crises



Source: Author's own elaborations

Note: Predicted probabilities shown in panel (a) correspond to the out-of-sample predictions derived from estimating the logit model in Column (3) of **Table 8** 1,000 times. Probabilities obtained from each replication are then averaged by country and year and their distribution plotted in panel (a). They are based on a total of 402 out-of-sample observations.

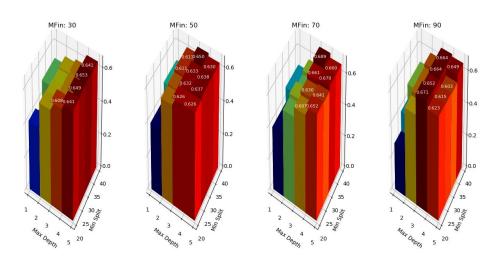
Logit model: ROC curves Figure 4 (a) Advanced economies (b) Emerging economies 1.00 0.75 0.75 0.50 0.50 0.25 0.25 0.00 0.00 0.00 0.25 0.50 0.75 1.00 1 - Specificity 0.00 0.25 0.75 1.00 0.50 1 - Specificity

Source: Author's own elaborations.

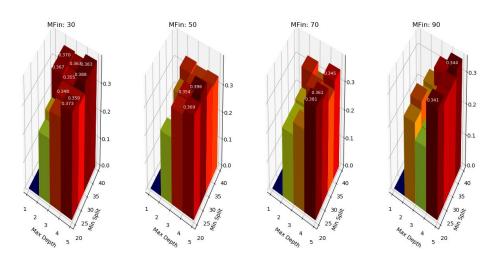
Note: The ROC curve shows the combination of sensitivity (or true positive rate) – y-axis – and 1-specificity (or false positive rate) – x-axis - at various cutoff settings. ROC curves in panel (a) and (b) are derived from results of the logit model in Column (3) of **Table 7** and **Table 8**, respectively. In particular, from the 1,000 replications we choose the one which yields an AUROC nearest to the average values shown in **Table 10**. Panel (a) plots the ROC curve for the out-of-sample advanced economies. The corresponding AUROC is equal to 0.75. Panel (b) shows the ROC curve calculated for the out-of-sample emerging economies. The corresponding AUROC is 0.78.

Figure 5 Grid analysis for Max Depth, Min Split, Number of Trees and Utility index

(a) Advanced Economies



(b) Emerging Economies

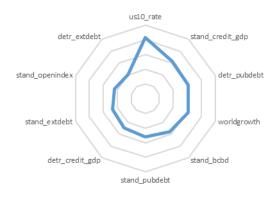


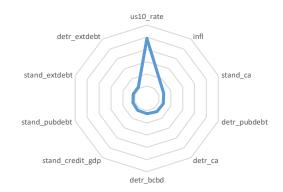
Source: Author's own elaborations.

Figure 6 Importance of variables in AdaBoost

Advanced Economies

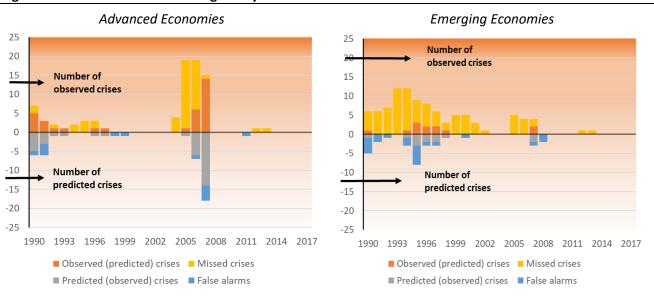
Emerging Economies





Source: Author's own elaborations.

Figure 7 AdoBoost: Forecasting ability



Source: Author's own elaborations.

Note: the upper panels display the subsample of observed crises, split into those that are correctly predicted (orange bars) and those that are incorrectly classified (i.e. missed, yellow bars). The lower panels display the subsample of predicted crises, split into the ones that were observed (grey bars) and the ones that are incorrectly classified (i.e. false alarms, blue bars). The yellow and the blue bars inform on how often the models fail to predict an observed crisis and on how often the models predict a false crisis, respectively. The absolute values of the orange and the grey bars provide the same information, i.e. the observed crises that are correctly predicted.

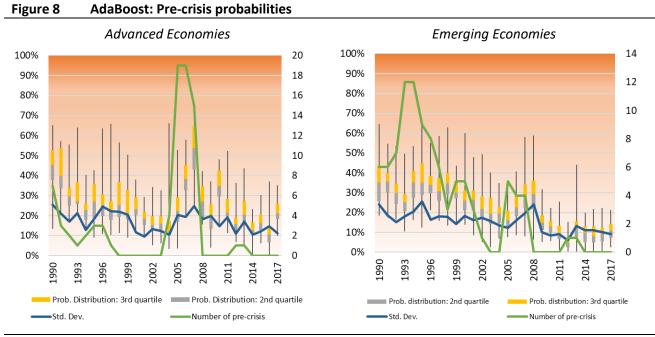
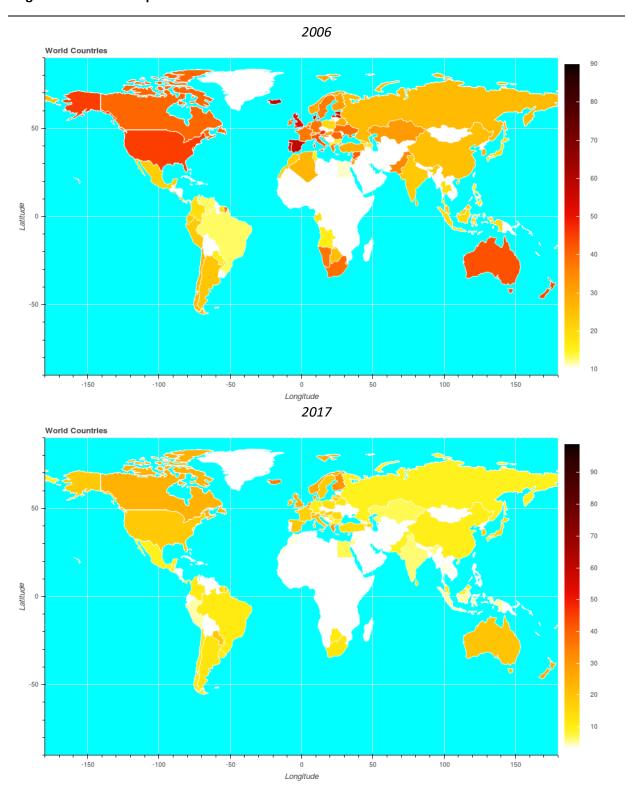


Figure 9 Heat maps



Appendix A Data and definitions

Table A1 Definitions of banking crises

Author	Definition
Caprio and Klingebiel (1997)	An episode of bank distress is systemic if much or all of the bank capital has been exhausted. Otherwise, it is classified as borderline. To distinguish between systemic banking crises and borderline cases, they also provide detailed information about NPLs, uncollectible loans, bank liquidations, revoked licences, takeover by the public sector and some other relevant variables.
Demirgüc-Kunt and Detragiache (1998, 2005)	An episode of distress is defined as a full-fledged crisis if at least one of the following four conditions holds: (1) the ratio of NPAs to total assets is higher than 10%; (2) the cost of the rescue operation is at least 2% of GDP; (3) a large-scale nationalization of banks has occurred; (4) bank runs take place or government measures (deposit freeze, deposit guarantees) are enacted.
Laeven and Valencia (2008, 2013, 2018)	A banking crisis is systemic if two conditions are met: "(1) Significant signs of financial distress in the banking system (significant bank runs, losses, bank liquidations); (2) Significant banking policy interventions in response to significant losses".
	When losses are severe, the first criterion is sufficient to date a systemic banking crisis. They consider that losses are severe when either (1) the share of NPLs is above 20 percent of total loans or bank closures of at least 20 percent of banking system assets or (2) fiscal restructuring costs of the banking sector are sufficiently high (> 5% of GDP).
	When quantifying the degree of financial distress is problematic or losses are mitigated by policy response, policy interventions are to be significant to date a crisis episode. A policy intervention is significant if at least three out of the following six measures were used: "(1) extensive liquidity support; (2) bank restructuring costs; (3) significant bank nationalizations; (4) significant guarantees; (5) significant asset purchases; (6) deposit freezes and bank holidays".
Reinhart and Rogoff (2009, 2011)	They mark a banking crisis by two types of events: (1) bank runs that lead to the closure, merging, or takeover by the public sector of one or more financial institutions; (2) if there are no runs, the closure, merging, takeovers, or large-scale government assistance of an important financial institution (or group of institutions) that marks the start of a string of similar outcomes for other financial institutions.
Schularick and Taylor (2012), Jordà et al. (2017a)	The focus is on the documentary descriptions contained in Bordo et al. (2001) and Reinhart and Rogoff (2009), two widely-used historical data sets that they compare and merge for a consistent definition of event windows. In line with the previous studies, they define a financial crisis when a country's banking sector experiences bank runs or sharp increases in default rates, accompanied by large losses of capital that result in public intervention, bankruptcy, or forced merger of financial institutions.
Baron et al. (2018)	They take the union of all crisis dates as the Joint Crisis List from many sources and uncover new banking crises that are not in existing databases but for which two criteria are satisfied: "(1) there is a decline in the bank equity index of at least 30%, and (2) there is an abundance of narrative evidence consistent with a banking crisis". Then, they remove spurious crises when both of the following criteria are met: (1) bank stock prices do not display a crash of at least 30%, and (2) we cannot find evidence in the historical record that there were either widespread bank failures or bank runs. By adding new crises and removing spurious crises, they create a revised chronology.

Table A2 List of countries included in the dataset, 1970-2017

Advanced economies

Denmark Estonia Finland France Germany Greece Azerbaijan Barbados Belarus Belize Bosnia and Hong Kong SAR Iceland Ireland Israel Italy Japan Korea Latvia Lithuania Luxembourg Netherlands New Zealand Norway Portugal Singapore Slovak Republic Slovenia Spain Sweden Switzerland **United Kingdom United States**

Emerging economies

Australia Austria Belgium Canada Czech Republic Albania Algeria Angola Argentina Armenia Herzegovina Botswana Brazil Brunei Bulgaria Chile China Colombia Costa Rica Croatia Dominican Republic Ecuador Egypt El Salvador Equatorial Guinea Fiji Gabon Georgia Guatemala Hungary India Indonesia Iran Jamaica Jordan Kazakhstan Kuwait Lebanon Libya Macedonia Malaysia Mauritius Mexico Morocco Namibia Pakistan Panama Paraguay Peru Philippines Poland Romania Russia Serbia Seychelles South Africa Sri Lanka Suriname Swaziland Syria Thailand Trinidad and Tobago Tunisia Turkey Turkmenistan Ukraine Uruguay Venezuela

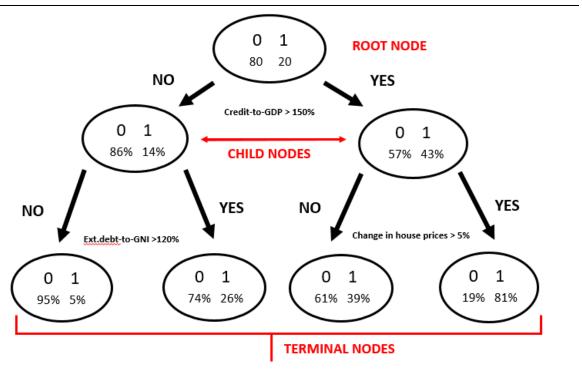
Table A3 Variable description and sources

Variable	Description	Source		
Country-specific				
Ratios				
Current Account-to-GDP	Current account balance, % of GDP	WB ^(a)		
External Debt-to-GNI	External debt stocks, % of GNI	WB, International Debt Statistics		
Public Debt-to-GDP	Gross general governement debt, % of GDP	IMF, Global Debt Database		
Openness Index	Sum of exports and imports of goods and services, % of GDP	WB ^(b)		
Credit-to-GDP	Credit to the private sector, % of GDP	BIS (WB when BIS data not available)		
Bank Credit-to-Bank Deposits	Private credit by deposit money banks, % of demand, time and saving deposits	WB, Financial Development and Structure Dataset (updated July 2018) and IMF, International Financial Statistics		
yoy % changes				
Inflation	GDP deflator, ratio of GDP in current local currency to GDP in constant local currency (yoy %)	WB ^(b)		
Real effective Exchange Rate	Real effective Exchange Rate based on CPI Index (yoy %)	WB ^(a)		
House price	Real house price index (yoy %)	BIS, FRED, OECD, Cesa-Bianchi (2013)		
Global				
Ratios				
10y US Treasury Rate	10-Year Treasury Constant Maturity Rate	Federal Reserve Dallas		
VIX	Volatility implied by S&P 500 index options	СВОЕ		
yoy % changes				
Energy Price Index	Average weighted prices of energy raw materials (weight = 4.7), crude oil (weight = 84.6) and natural gas (weight = 10.8) (yoy %)	World Bank Commodity Price Data		
Real World GDP growth	Annual percentage growth rate of world GDP at constant prices (yoy %)	WB ^(b)		

Source: Authors' own elaborations based on BIS, CBOE, IMF and WB.

Notes: (a) WB cites as source "International Monetary Fund, Balance of Payments Statistics Yearbook and data files, and World Bank and OECD GDP estimates"; (b) WB cites as source "National accounts data and OECD National Accounts"

Figure A1 Binary classification tree: an example



Appendix B Robustness analysis

Table B1 Marginal effects: Robustness for advanced economies, 1970-2017						
	(1)	(2)	(3)	(4)	(5)	
	crisis	precrisis (2a)	precrisis (2b)	precrisis (2b)	precrisis (2b)	
					1992-2017	
Real GDP growth	0.005**	0.008	0.005	0.005	-0.011	
	(0.002)	(0.005)	(0.005)	(0.005)	(0.008)	
Current account-to-GDP	0.001	-0.005	-0.002	-0.002	-0.012	
	(0.005)	(0.012)	(0.014)	(0.014)	(0.015)	
External debt-to-GNI	0.028***	0.037***	0.047***	0.047*	0.046***	
	(0.004)	(0.009)	(0.012)	(0.028)	(0.010)	
Public debt-to-GDP	-0.032***	-0.087***	-0.092***	-0.092***	-0.094***	
	(0.007)	(0.014)	(0.016)	(0.016)	(0.021)	
Credit-to-GDP	0.011**	0.005	0.017	0.017	0.032**	
	(0.005)	(0.013)	(0.015)	(0.015)	(0.015)	
10y US Treasury rate	0.005**	0.009*	0.010	0.010*	0.051***	
	(0.002)	(0.005)	(0.006)	(0.006)	(0.016)	
Real world GDP growth	0.006*	0.020**	0.021**	0.021**	0.098***	
	(0.003)	(0.008)	(0.008)	(0.008)	(0.019)	
External debt-to-GNI*US 10y Treasury						
rate				0.000		
				(0.005)		
VIX max					-0.015***	
					(0.002)	
Country dummies	YES	YES	YES	YES	YES	
No. obs.	1,089	1,070	931	931	493	
Pseudo R-squared	0.270	0.213	0.231	0.231	0.554	
AUROC	0.862	0.801	0.804	0.804	0.951	

Note: In Column (1) crisis = 1 identifies the year when the crisis occurs, 0 otherwise, and the set of explanatory variables are taken at t-1. In Column (2) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise. In Columns (3)-(5) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise except post-crisis years. From Columns (2) to (5) explanatory variables are taken at time t. All variables are detrended and standardised, with the exception of Current account-to-GDP (only standardised), Real GDP growth, 10y US Treasury rate, Real world GDP growth and VIX max. In Column (5) the logit is applied to data as of 1992 since the VIX is only available from that date forward. The AUROC is the area under receiving operating characteristic. Standard errors in brackets are clustered at the country level. * p<0.05; ** p<0.01; ***p<0.001.

Table B2 Marginal effects: Robustness for emerging economies, 1970-2017 (1) (2)(3) (4)(5)crisis precrisis (2a) precrisis (2b) precrisis (2b) precrisis (2b) 1992-2017 -0.005*** Real GDP growth -0.001 -0.004** -0.005*** -0.005** (0.001)(0.001)(0.002)(0.002)(0.002)-0.024*** Current account-to-GDP -0.007* -0.011 -0.010 -0.011 (0.004)(0.009)(0.011)(0.011)(0.009)External debt-to-GNI -0.011 -0.005 -0.054*** -0.014 -0.001 (0.006)(0.013)(0.014)(0.02)(0.014)Public debt-to-GDP -0.016*** -0.026** -0.031** -0.035** -0.034*** (0.012)(0.014)(0.014)(0.013)(0.006)0.000* 0.000 Inflation 0.000 0.000 -0.000 (0.000)(0.000)(0.000)(0.000)(0.000)0.005*** 0.014*** 0.019*** 0.021*** 0.037*** 10y US Treasury rate (0.001)(0.002)(0.003)(0.003)(0.006)Real world GDP growth 0.002 0.009** 0.008** 0.007* -0.003 (0.003)(0.004)(0.004)(0.004)(0.006)External debt-to-GNI*US 10y Treasury rate 0.007*** (0.002)-0.002*** VIX max (0.001)Region dummies YES YES YES YES YES No. obs. 2,273 2,244 2,010 2,010 1,292 Pseudo R-squared 0.128 0.139 0.172 0.180 0.368 0.795 0.812 AUROC 0.803 0.817 0.920

Note: In Column (1) crisis = 1 identifies the year when the crisis occurs, 0 otherwise, and the set of explanatory variables are taken at t-1. In Column (2) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise. In Columns (3)-(5) pre-crisis = 1 identifies the 3 years preceding a crisis, 0 otherwise except post-crisis years. From Columns (2) to (5) explanatory variables are taken at time t. All variables are detrended and standardised, with the exception of Real GDP growth, Current account-to-GDP (only standardised), Inflation, 10y US Treasury rate, Real world GDP growth and VIX max. In Column (5) the logit is applied to data as of 1992 since the VIX is only available from that date forward. The AUROC is the area under receiving operating characteristic. Standard errors in brackets are clustered at the region level. * p<0.05; ***p<0.01; ***p<0.001.